## SUCCESS

is When Your
signature
changes to Autograph

## 1. RELATIONS AND FUNCTION

## 5 MARKS

If $f(x)=2 x+3, g(x)=1-2 x$ and $\mathrm{h}(x)=3 x$. Prove that $f \circ(g \circ h)=(f \circ g) \circ h$.
Solution: $f(x)=2 x+3, g(x)=1-2 x, h(x)=3 x$

$$
(f \circ g)=2(1-2 x)+3=2-4 x+3=5-4 x
$$

$(f \circ g) \circ h=5-4(3 x)=5-12 x \quad \ldots .(1)$
$(g \circ h)=1-2(3 x)=1-6 x$
$f \circ(g \circ h)=2(1-6 x)+3=5-12 x \cdots .(2)$
From (1) and (2) $\Rightarrow f \circ(g \circ h)=(f \circ g) \circ h$.

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If f(x)=\frac{x+6}{3}\mathrm{ and g(x)=3-x, find fog and gof. Check whether fog=g of.}
Solution: }\mp@subsup{}{}{3
(f\circg)=\frac{(3-x)+6}{3}=\frac{9-x}{3}
(g\circf)=3-\frac{x+6}{3}=\frac{3-x}{3}
From (1) and (2) =>f f\circg\not=g\circf.
If f(x)=x-4,g(x)=\mp@subsup{x}{}{2}}\mathrm{ and h(x)=3x-5, Prove that fo(g०h)=(f०g) ○h.
Solution:
    (f\circg)}=\mp@subsup{x}{}{2}-
    \therefore((f\circg)\circh)=(3x-5)2-4 \ldots.(1)
        (g\circh)=(3x-5)}\mp@subsup{)}{}{2
    \therefore(f\circ (g\circh)=(3x-5)\mp@subsup{)}{}{2}-4 ...(2)
                                    From (1) and (2)
                                    #(f\circg)\circh=f\circ(g\circh)
If f(x)=\mp@subsup{x}{}{2},g(x)=2x and h(x)=(x+4), Prove that f\circ(g\circh)=(f\circg)\circh.
Solution: (fog)=(2x)}\mp@subsup{)}{}{2}=4\mp@subsup{x}{}{2
    \therefore((f\circg)\circh)=4(x+4)2 ...(1)
        (g\circh):=2(x+4)
    \therefore(f\circ(g\circh)=(2(x+4))\mp@subsup{)}{}{2}=4(x+4)\mp@subsup{)}{}{2}\ldots(2)
        From (1) and (2) }=>(f\circg)\circh=f\circ(g\circh
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STUDY MATERIAL
A.ABDULMUNAB M.SC.,B.ED.,
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JAYANKONDAM,
ARIYALUR DT.
CELL:9524103797



| If the function $f: \mathrm{R} \rightarrow \mathrm{R}$ defined by then find the values of |
| :--- |
| (i) $\mathrm{f}(4)$ (ii) $\mathrm{f}(-2)$ (iii) $\mathrm{f}(4)+2 \mathrm{f}(1)$ |
| (iv) $\frac{f(1)-3 f(4)}{f(-3)}$ |
| Solution: |\(\quad f(x)=\left\{\begin{array}{l}2 x+7, x<-2 <br>

x^{2}-2,-2 \leq x<3, <br>
3 x-2, x \geq 3\end{array}\right.\)

Solution :
(i) $f(4)=12-2=10$
(ii) $f(-2)=4-2=2$
(iii) $f(4)+2 f(1)=10-2=8$
(iv) $\frac{f(1)-3 f(4)}{f(-3)}=-31$

A function $f:[-5,9] \rightarrow R$ is defined as follows: Find (i) $f(-3)+f(2) \quad$ (ii) $f(7)-f(1)$
$f(x)=\left\{\begin{array}{lll}6 x+1 & \text { if }-5 \leq x<2 \\ 5 x^{2}-1 & \text { if } & 2 \leq x<6\end{array}\right.$
(iii) $2 f(4)+f(8)$
(iv) $\frac{2 f(-2)-f(6)}{f(4)+f(-2)}$
$3 x-4$ if $6 \leq x<6$

Solution :
(ii) $f(7)-f(1)=17-7=10$
(iii) $2 f(4)+f(8)=178$
(iv) $\frac{2 f(-2)-f(6)}{f(4)+f(-2)}=\frac{-9}{17}$

(ii) $f(0)=2$ (iii) $f(-1.5)=-1.5-1=-2.5$ (iv) $f(2)+f(-2)=4-3=1$

Let $A=$ The set of all natural numbers less than $8, B=$ The set of all prime numbers less than 8
$C=$ The set of even prime number. Verify that $A \times(B-C)=(A \times B)-(A \times C)$
Solution: $\mathrm{A}=\{1,2,3,4,5,6,7\}, \mathrm{B}=\{2,3,5,7\}$ and $\mathrm{C}=\{2\}$

$$
B-C=\{3,5,7\}-\{2\}=\{3,5,7\}
$$

A ZAYAAN ABDUL M.SC. EED.
$\therefore A \times(B-C)=\{1,2,3,4,5,6,7\} \times\{3,5,7\}$

$$
\begin{equation*}
=\{(1,3),(1,5),(1,7),(2,3),(2,5),(2,7),(3,3),(3,5),(3,7),(4,3),(4,5),(4,7), \tag{5,3}
\end{equation*}
$$

$A \times B=\{1,2,3,4,5,6,7\} \times\{2,3,5,7\}$
$=\{(1,2),(1,3),(1,5),(1,7),(2,2),(2,3),(2,5),(2,7),(3,2),(3,3),(3,5),(3,7)$, $(4,2),(4,3),(4,5),(4,7),(5,2),(5,3),(5,5),(5,7),(6,2),(6,3),(6,5),(6,7)$, $(7,2),(7,3),(7,5),(7,7)$,
$A \times C=\{1,2,3,4,5,6,7\} \times\{2\}=\{(1,2),(2,2),(3,2),(4,2),(5,2),(6,2),(7,2)\}$
$\therefore(A \times B)-(A \times C)=\{(1,3),(1,5),(1,7),(2,3),(2,5),(2,7),(3,3),(3,5),(3,7),(4,3),(4,5),(4,7)$,
$(5,3),(5,5),(5,7),(6,3),(6,5),(6,7),(7,3),(7,5),(7,7)$,

## The function ' $t$ ' which maps temperature in Celsius (C) into temperature in Fahrenheit ( $F$ ) is defined

 by $t(C)=F$ where $F=\frac{9}{5} C+32$, Find, (i) $t(0)$ (ii) $t(28)$ (iii) $t(-10)$ (iv) the value of $C$ when $t(C)=212$ (v) the temperature when the Celsius value is equal to the Farenheit value.Solution : Given $\mathrm{t}(\mathrm{C})=\mathrm{F}=\frac{9 C}{5}+32$
(i) $t(0)=\frac{9(0)}{5}+32=32^{\circ} \mathrm{F}$
(ii) $t(28)=\frac{9(28)}{5}+32=82.4^{\circ} \mathrm{F}$
(iii) $t(-10)=\frac{9(-10)}{5}+32=14^{\circ} \mathrm{F}$
(iv) When $t(c)=212 \Rightarrow 212=\frac{9 C}{5}+32 \Rightarrow C=100^{\circ} \mathrm{C}$
(v) When Celsius value $=$ Farenheit value $\Rightarrow C=\frac{9 C}{5}+32 \Rightarrow C=-40^{\circ}$


Let $A=\{x \in W \mid x<2\}, B=\{x \in N \mid 1<x \leq 4\}$ and $C=\{3,5\}$. Verify that $A \times(B \cup C)=(A \times B) \cup(A \times C)$
Solution : $A=\{x \in W \mid x<2\} \Rightarrow A=\{0,1\} \quad B=\{x \in N \mid 1<x \leq 4\} \Rightarrow B=\{2,3,4\} \quad C=\{3,5\}$ $B \cup C=\{2,3,4\} \cup\{3,5\}=\{2,3,4,5\}$
$\therefore A \times(B \cup C)=\{0,1\} \times\{2,3,4,5\}=\{(0,2),(0,3),(0,4),(0,5),(1,2),(1,3),(1,4),(1,5)\} \ldots(1)$
$\mathrm{A} \times \mathrm{B}=\{0,1\} \times\{2,3,4\}=\{(0,2),(0,3),(0,4),(1,2),(1,3),(1,4)\}$
$A \times C=\{0,1\} \times\{3,5\}=\{(0,3),(0,5),(1,3),(1,5)\}$
$\therefore(\mathrm{A} \times \mathrm{B}) \cup(\mathrm{A} \times \mathrm{C})=\{(0,2),(0,3),(0,4),(0,5),(1,2),(1,3),(1,4),(1,5)\} \ldots(2)$
$\therefore$ From (1) and (2) $\mathbf{A} \times(\mathbf{B} \cup \mathbf{C})=(\mathbf{A} \times \mathbf{B}) \cup(\mathbf{A} \times \mathbf{C})$
Let $A=\{x \in W \mid x<2\}, B=\{x \in N \mid 1<x \leq 4\}$ and $C=\{3,5\}$. Verify that $A \times(B \cap C)=(A \times B) \cap(A \times C)$ Solution : $\mathrm{A}=\{x \in \mathrm{~W} \mid x<2\} \Rightarrow \mathrm{A}=\{0,1\}, \mathrm{B}=\{x \in \mathrm{~N} \mid 1<x \leq 4\} \Rightarrow \mathrm{B}=\{2,3,4\}$ and $\mathrm{C}=\{3,5\}$ $B \cap C=\{2,3,4\} \cap\{3,5\}=\{3\}$
$\therefore \mathrm{A} \times(\mathrm{B} \cap \mathrm{C})=\{0,1\} \times\{3\}=\{(0,3),(1,3)\} \quad \ldots(1)$
$\mathbf{A} \times \mathbf{B}=\{0,1\} \times\{2,3,4\}=\{(0,2),(0,3),(0,4),(1,2),(1,3),(1,4)\}$
$A \times C=\{0,1\} \times\{3,5\}=\{(0,3),(0,5),(1,3),(1,5)\}$
$\therefore(\mathrm{A} \times \mathrm{B}) \cap(\mathrm{A} \times \mathrm{C})=\{(0,3),(1,3)\} \quad \ldots(2)$
$\therefore$ From (1) and (2), $A \times(B \cap C)=(A \times B) \cap(A \times C)$

## A ZAYAAN ABDUL M.SC., BED.

Let $A=\{x \in W \mid x<2\}, B=\{x \in N \mid 1<x \leq 4\}$ and $C=\{3,5\}$. Verify that $(A \cup B) \times C=(A \times C) \cup(B \times C)$
Solution : $\mathrm{A}=\{x \in \mathrm{~W} \mid x<2\} \Rightarrow \mathrm{A}=\{0,1\}, \mathrm{B}=\{x \in \mathrm{~N} \mid 1<x \leq 4\} \Rightarrow \mathrm{B}=\{2,3,4\}$ and $\mathrm{C}=\{3,5\}$

$$
A \cup B=\{0,1\} \cup\{2,3,4\}=\{0,1,2,3,4\}
$$

$(A \cup B) \times C=\{(0,3),(0,5),(1,3),(1,5),(2,3),(2,5),(3,3),(3,5),(4,3),(4,5)\} \ldots(1)$

$$
A \times C=\{0,1\} \times\{3,5\}=\{(0,3),(0,5),(1,3),(1,5)\}
$$

$B \times C=\{2,3,4\} \times\{3,5\}=\{(2,3),(2,5),(3,3),(3,5),(4,3),(4,5)\}$
$(A \times C) \cup(B \times C)=\{(0,3),(0,5),(1,3),(1,5),(2,3),(2,5)(3,3),(3,5),(4,3),(4,5)\}$ $\therefore$ From (1) and (2) $(\mathbf{A} \cup \mathbf{B}) \times \mathbf{C}=(\mathbf{A} \times \mathbf{C}) \cup(\mathbf{B} \times \mathbf{C})$
Let $\mathrm{A}=\{x \in \mathrm{~N} \mid 1<x<4\}, \mathrm{B}=\{x \in \mathrm{~W} \mid 0 \leq x<2\}$ and $\mathrm{C}=\{x \in \mathrm{~N} \mid x<3\}$.
verify that $\mathrm{A} \times(\mathrm{B} \cup \mathrm{C})=(\mathrm{A} \times \mathrm{B}) \cup(\mathrm{A} \times \mathrm{C})$
Solution : $\mathrm{A}=\{x \in \mathrm{~N} \mid 1<x<4\}=\{2,3\}, \mathrm{B}=\{x \in \mathrm{~W} \mid 0 \leq x<2\}=\{0,1\}$ and $\mathrm{C}=\{x \in \mathrm{~N} \mid x<3\}=\{1,2\}$ $B \cup C=\{0,1\} \cup\{1,2\}=\{0,1,2\}$
$A \times(B \cup C)=\{2,3\} \times\{0,1,2\}=\{(2,0),(2,1),(2,2),(3,0),(3,1),(3,2)\} \ldots(1)$
$\mathrm{A} \times \mathrm{B}=\{2,3\} \times\{0,1\}=\{(2,0),(2,1),(3,0),(3,1)\}$
$A \times C=\{2,3\} \times\{1,2\}=\{(2,1),(2,2),(3,1),(3,2)\}$
$(A \times B) \cup(A \times C)=\{(2,0),(2,1),(3,0),(3,1)\} \cup\{(2,1),(2,2),(3,1),(3,2)\}$

$$
=\{(2,0),(2,1),(2,2),(3,0),(3,1),(3,2)\} \ldots(2)
$$

From (1) and (2), $A \times(B \cup C)=(A \times B) \cup(A \times C)$ is verified.
Let $\mathrm{A}=\{x \in \mathrm{~N} \mid 1<x<4\}, \mathrm{B}=\{x \in \mathrm{~W} \mid 0 \leq x<2\}$ and $\mathrm{C}=\{x \in \mathrm{~N} \mid x<3\}$.
verify that $\mathrm{A} \times(\mathrm{B} \cap \mathrm{C})=(\mathrm{A} \times \mathrm{B}) \cap(\mathrm{A} \times \mathrm{C})$
Solution : $\mathrm{A}=\{x \in \mathrm{~N} \mid 1<x<4\}=\{2,3\}, \mathrm{B}=\{x \in \mathrm{~W} \mid 0 \leq x<2\}=\{0,1\}$ and $\mathrm{C}=\{x \in \mathrm{~N} \mid x<3\}=\{1,2\}$ $B \cap C=\{0,1\} \cap\{1,2\}=\{1\}$
$\mathrm{A} \times(\mathrm{B} \cap \mathrm{C})=\{2,3\} \times\{1\}=\{(2,1),(3,1)\} \ldots(1)$
$A \times B=\{2,3\} \times\{0,1\}=\{(2,0),(2,1),(3,0),(3,1)\}$
$A \times C=\{2,3\} \times\{1,2\}=\{(2,1),(2,2),(3,1),(3,2)\}$
$(\mathrm{A} \times \mathrm{B}) \cap(\mathrm{A} \times \mathrm{C})=\{(2,0),(2,1),(3,0),(3,1)\} \cap\{(2,1),(2,2),(3,1),(3,2)\}=\{(2,1),(3,1)\} \ldots(2)$
From (1) and (2), $A \times(B \cap C)=(A \times B) \cap(A \times C)$ is verified.

Let $f: A \rightarrow B$ be a function define by. $f(x)=\frac{x}{2}-1$ where $A=\{2,4,6,10,12\}, B=\{0,1,2,4,5,9\}$.
Represent $f$ by (i) set of ordered pairs ; (ii) a table ; (iii) an arrow diagram; (iv) a graph
Solution : Given $f(x)=\frac{x}{2}-1$
(iii) Arrow diagram :

$$
\begin{array}{rl}
f(2)=0 & f(4)=1 \\
f(6)=2 & f(10)=4 \\
f(12)=5 &
\end{array}
$$

(i) Set of order pairs :
$f=\{(2,0),(4,1),(6,2),(10,4),(12,5)\}$
(iv) Graph
ii) Table



Let $\mathrm{A}=\{1,2,3,4\}$ and $\mathrm{B}=\{2,5,8,11,14\}$ be two sets. Let $f: \mathrm{A} \rightarrow \mathrm{B}$ be a function given by $\mathrm{f}(x)=3 x-1$. Represent this function (i) by arrow diagram $\quad$ (ii) in a table form
(iii) as a set of ordered pairs (iv) in a graphical form

Solution:
(iv) Graphical form
$\mathrm{A}=\{1,2,3,4\} ; \mathrm{B}=\{2,5,8,11,14\}$
(i) Arrow diagram
$\mathrm{f}(\mathrm{x})=3 \mathrm{x}-1$
$\mathrm{f}(\mathrm{l})=2$;
$f(2)=5$
$\mathrm{f}(3)=8$;
$\mathrm{f}(4)=11$
(ii) Table form

| $x$ | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{f}(x)$ | 2 | 5 | 8 | 11 |


(iii) Set of ordered pairs
$f=\{(1,2),(2,5),(3,8),(4,11)\}$


## 2.NUMBERS AND SEQUENCES

5 MARKS
Find the sum of $9^{3}+10^{3}+\ldots . .+21^{3}$ A ZAYAAN ABDUL M.SC., BEDD.
JAYANKONDAM, ARIYAIUR DT.

Solution: $9^{3}+10^{3}+\ldots .+21^{3}$

$$
\left[\frac{21 \times(21+1)}{2}\right]^{2}-\left[\frac{8 \times(8+1)}{2}\right]^{2}=(231)^{2}-(36)^{2}=52065\left[\therefore \sum_{k=1}^{n} K^{3}=\left(\frac{n(n+1)}{2}\right)^{2}\right]
$$

Find the sum of $5^{2}+10^{2}+15^{2}+\ldots .+105^{2}$
Solution : $\begin{aligned} 5^{2}+10^{2}+15^{2}+\ldots .+105^{2} & =5^{2}\left(1^{2}+2^{2}+3^{2}+\ldots .+21^{2}\right) \\ & =\frac{25 \times 21 \times 22 \times 43}{6}=82775\end{aligned} \quad\left[\therefore \sum_{k=1}^{n} K^{2}=\frac{n(n+1)(2 n+1)}{6}\right]$
Find the sum of $15^{2}+16^{2}+17^{2}+\ldots .28^{2}$
Solution: $15^{2}+16^{2}+17^{2}+\ldots .28^{2}$

$$
\frac{28 \times 29 \times 57}{6}-\frac{14 \times 15 \times 29}{6}=7714-1015=6699\left[\therefore \sum_{k=1}^{n} K^{2}=\frac{n(n+1)(2 n+1)}{6}\right]
$$

Rekha has 15 square colour papers of sizes $10 \mathrm{~cm}, 11 \mathrm{~cm}, 12 \mathrm{~cm}, \ldots, 24 \mathrm{~cm}$. How much are can be decorated with these colour papers?
Solution : $10 \mathrm{~cm}, 11 \mathrm{~cm}, 12 \mathrm{~cm}, \ldots . . . . .24 \mathrm{~cm}$
$10^{2}+11^{2}+12^{2}+\ldots \ldots . .+24^{2}=\frac{24 \times 25 \times 49}{6}-\frac{9 \times 10 \times 19}{6}=4615 \mathrm{~cm}^{2}$

$$
\left.\therefore \sum_{k=1}^{n} K^{2}=\frac{n(n+1)(2 n+1)}{6}\right]
$$

The sum of first, $n, 2 n$ and $3 n$ terms of an A.P. are $S_{1}, S_{2}$ and $S_{3}$ respectively. Prove that $S_{3}=3\left(S_{2}-S_{1}\right)$.
Solution : $S_{1}=t_{1}=a, \quad S_{2}=a+a+d=2 a+d, S_{3}=a+a+d+a+2 d=3 a+3 d$

$$
\therefore 3\left(S_{2}-S_{1}\right)=3 a+3 d=S_{3}
$$

The houses of a street are numbered from 1 to 49 . Senthil's house is numbered such that the sum of numbers of the houses prior to Senthil's house is equal to the sum of numbers of the houses following Senthil's house. Find Senthil's house number?
Solution : Let Senthil's house number be $x . \quad \frac{x(x-1)}{2}+\frac{x(x+1)}{2}=\frac{49 \times 50}{2} \Rightarrow x^{2}=35^{2}\left[\therefore S_{n}=n / 2[a+l]\right]$
Find the sum of $\mathbf{1 0}^{\mathbf{3}}+\mathbf{1 1}^{\mathbf{3}}+\mathbf{1 2}^{\mathbf{3}}+\ldots . .+\mathbf{2 0 ^ { 3 }}$
$\begin{aligned} 10^{3}+11^{3}+12^{3}+\ldots . .+20^{3} & =\left(1^{3}+2^{3}+\ldots \ldots .+20^{3}\right)-\left(1^{3}+2^{3}+\ldots \ldots . .+9^{3}\right) \quad\left(\sum_{k=1}^{n} K^{3}=\left(\frac{n(n+1)}{2}\right)^{2}\right) \\ & =\left(\frac{20 \times 21}{2}\right)^{2}-\left(\frac{9 \times 10}{2}\right)^{2}=42075\end{aligned}$
ind the sum to $n$ terms of the series $5+55+555+$..
Find the sum to $n$ terms of the series $5+55+555+\ldots$
Solution $: 5+55+555+\ldots .+n$ terms $=5[1+11+111+\ldots .+\mathrm{n}$ terms $]=\frac{5}{9}\left[\frac{10\left(10^{n}-1\right)}{(10-1)}-n\right]\left[S_{n}=a \cdot \frac{r^{n}-1}{r-1}\right.$
A ZAYAAN ABDUL M.SC.EBD.,
JAYANIKONDAM,ARIYALUR DT.
Find the sum to $n$ terms of the series $0.4+0.44+0.444+\ldots .$. to $n$ terms
Solution :
$0.4+0.44+0.444+\ldots . . .$. to $n$ terms $=\frac{4}{10}+\frac{44}{100}+\frac{444}{1000}+$

Find the sum to $n$ terms of the series $3+33+333+\ldots \ldots$. to $n$ terms
Solution $3(1+11+111+\ldots \ldots .+n$ terms $)=\frac{3}{9}(9+99+999+\ldots \ldots \ldots+n$ terms $)=\frac{3}{9}\left[\frac{10\left(10^{n}-1\right)}{(10-1)}-n\right]\left[S_{n}=a \cdot \frac{r^{n}-1}{r-1}\right.$
Kumar writes a letter to four of his friends. He asks each one of them to copy the letter and mail to four different persons with the instruction that they con tinue the process similarly. Assuming that the process is unaltered and it costs ₹ 2 to mail one letter, spent on find the amount postage when $8^{\text {th }}$ set of letters is mailed.

$$
\begin{aligned}
& \text { find the amount postage when } 8^{\text {ti }} \text { set of letters is mailed. } \\
& \text { Solution : The total cost }=(4 \times 2)+(16 \times 2)+(64 \times 2)+\ldots . . . . .8^{\text {m }} \text { set }=8 \cdot \frac{4^{8}-1}{3}=\bar{₹} 174760\left[\therefore S_{n}=a \cdot \frac{r^{n}-1}{r-1}\right.
\end{aligned}
$$

If $S_{n}=(x+y)+\left(x^{2}+x y+y^{2}\right)+\left(x^{3}+x^{2} y+x y^{2}+y^{3}\right)+\ldots . . . . . n$ terms then prove that
$(x-y) S_{n}=\left|\frac{x^{2}\left(x^{n}-1\right)}{x-1}-\frac{y^{2}\left(y^{n}-1\right)}{y-1}\right|$
Solution: $\quad(x-y) S_{n}=\left(x^{2}+x^{3}+x^{4}+\ldots \ldots . . n\right.$ terms $)-\left(y^{2}+y^{3}+y^{4}+\ldots \ldots . . n\right.$ terms $)$

$$
=\frac{x^{2}\left(x^{n}-1\right)}{x-1}-\frac{y^{2}\left(y^{n}-1\right)}{y-1}
$$

## 5 MARKS <br> 3. ALGEBRA

Find the square root of $\left(6 \mathrm{x}^{2}+\mathrm{x}-1\right)\left(3 \mathrm{x}^{2}+2 \mathrm{x}-1\right)\left(2 \mathrm{x}^{2}+3 \mathrm{x}+1\right)$
Solution : $\sqrt{\left(6 x^{2}+x-1\right)\left(3 x^{2}+2 x-1\right)\left(2 x^{2}+3 x+1\right)}=\sqrt{(3 x-1)(2 x+1)(3 x-1)(x+1)(2 x+1)(x+1)}$

$$
=|(3 x-1)(2 x+1)(x+1)|
$$

Find the square root of $\left(4 x^{2}-9 x+2\right)\left(7 x^{2}-13 x-2\right)\left(28 x^{2}-3 x-1\right)$
Solution : $\sqrt{\left(4 x^{2}-9 x+2\right)\left(7 x^{2}-13 x-2\right)\left(28 x^{2}-3 x-1\right)}=\sqrt{(4 x-1)(x-2)(7 x+1)(x-2) \cdot(7 x+1)(4 x-1)}$

$$
=|(7 x+1)(4 x-1)(x-2)|
$$

Find the square root of the following $\left(2 x^{2}+\frac{17}{6} x+1\right)\left(\frac{3}{2} x^{2}+4 x+2\right)\left(\frac{4}{3} x^{2}+\frac{11}{3} x+2\right)$
Solution:

$$
\begin{aligned}
& =1 / 6 \sqrt{(4 x+3)^{2} \cdot(3 x+2)^{2} \cdot(x+2)^{2}} \\
& =1 / 6|(4 x+3)(3 x+2)(x+2)|
\end{aligned}
$$

Simplify $\frac{1}{x^{2}-5 x+6}+\frac{1}{x^{2}-3 x+2}-\frac{1}{x^{2}-8 x+15}$
Solution :

$$
\begin{aligned}
\frac{1}{x^{2}-5 x+6}+\frac{1}{x^{2}-3 x+2}-\frac{1}{x^{2}-8 x+15} & =\frac{1}{(x-2)(x-3)}+\frac{1}{(x-2)(x-1)}-\frac{1}{(x-5)(x-3)} \\
& =\frac{(x-9)(x-2)}{(x-1)(x-2)(x-3)(x-5)}=\frac{x-9}{(x-1)(x-3)(x-5)}
\end{aligned}
$$

The number of seats in a row is equal to the total number of rows in a hall. The total number of seats in the hall will increase by 375 if the number of rows is doubled and the number of seats in each row is reduced by 5 . Find the number of rows in the hall at the beginning.
Solution: Let the number of rows be x .
$\therefore$ Number of seats in each row $=\mathrm{x} \quad \therefore$ Total number of seats in the hall $=\mathrm{x}^{2}$
$\therefore$ By the data given, $2 x \times(x-5)=x^{2}+375$

$$
\therefore \quad \mathrm{x}=25,-15 \quad \therefore \text { No. of rows at the beginning }=25 \text {. }
$$

From a group of $\mathbf{2 x}{ }^{\mathbf{2}}$ black bees, square root of half of the group went to a tree. Again eight-ninth of the bees went to the same tree. The remaining two got caught up in a fragrant lotus.
How many bees were there in total?
Solution: Given number of black bees $=2 \mathrm{x}^{2}$
By the data given, $\quad 2 x^{2}-x-8 / 9\left(2 x^{2}\right)=2 \Rightarrow x=6,-3 / 2$ $\therefore x=6$
. Total number of bees $=2 \mathrm{x}^{2}=2(36)=72$
A flock of swans contained $x^{2}$ members. As the clouds gathered, $10 x$ went to a lake and one eighth of the members flew away to a garden. The remaining three pairs played about in the water.

How many swans were there in total?
Solution: A flock of swans contained $\mathrm{x}^{2}$ members.

## JAYANKON DAM,ARIYALUR DT.

$$
x^{2}-10 x-\frac{1}{8} x^{2}=6 \Rightarrow \mathrm{x}=12 . \quad \text { Total number of swans is } \mathrm{x}^{2}=144
$$

Find the square root of $\left[\sqrt{15} x^{2}+(\sqrt{3}+\sqrt{10}) x+\sqrt{2}\right]\left[\sqrt{5} x^{2}+(2 \sqrt{5}+1) x+2\right]\left[\sqrt{3} x^{2}+(\sqrt{2}+2 \sqrt{3}) x+2 \sqrt{2}\right]$ Solution:

$$
\sqrt{(\sqrt{5} x+1)(\sqrt{3} x+\sqrt{2})(\sqrt{5} x+1)(x+2)(\sqrt{3} x+\sqrt{2})(x+2)}=|(\sqrt{5} x+1)(\sqrt{3} x+\sqrt{2})(x+2)|
$$



If $4 x^{4}-12 x^{3}+37 x^{2}+b x+a$ is perfect square, Find the values of $a$ and $b$
Solution :


If $a x^{4}+b x^{3}+361 x^{2}+220 x+100$ is perfect square,
Find the values of $a$ and $b$
Solution :
$20 \quad 22$


If $\frac{1}{x^{4}}-\frac{6}{x^{3}}+\frac{13}{x^{2}}+\frac{m}{x}+n$ is perfect square,
Find the values of $m$ and $n$
Solution :


If $x^{4}-8 x^{3}+m x^{2}+n x+16$ is perfect square, Find the values of $m$ and $n$


Find $\sqrt{64 x^{4}-16 x^{3}+17 x^{2}-2 x+1}$
Solution:

$\sqrt{64 x^{4}-16 x^{3}+17 x^{2}-2 x+1}=\left|8 x^{2}-x+1\right|$
A ZAYAAN ABDUL M.SC.,BED, JAYANICONDAM,ARIYALUR DT.


## 3. MATRICE

Find $X$ and $Y$ if $X+Y=\left(\begin{array}{ll}7 & 0 \\ 3 & 5\end{array}\right)$ and $\mathbf{X}-\mathbf{Y}=\left(\begin{array}{ll}3 & 0 \\ 0 & 4\end{array}\right)$

$$
\begin{array}{ll}
\text { Solution : } \\
& \mathrm{X}+\mathrm{Y}=\left(\begin{array}{ll}
7 & 0 \\
3 & 5
\end{array}\right) \cdots \ldots \ldots .(1) \quad \mathrm{X}-\mathrm{Y}=\left(\begin{array}{ll}
3 & 0 \\
0 & 4
\end{array}\right) \ldots \ldots . . . .(2) \\
(\mathrm{l})+(2) \Rightarrow 2 \mathrm{X}=\left(\begin{array}{ll}
10 & 0 \\
3 & 9
\end{array}\right) \Rightarrow \mathrm{X}=\left(\begin{array}{cc}
5 & 0 \\
3 / 2 & 9 / 2
\end{array}\right) \quad(1)-(2) \Rightarrow 2 \mathrm{Y}=\left(\begin{array}{ll}
4 & 0 \\
3 & 1
\end{array}\right) \Rightarrow \mathrm{Y}=\left(\begin{array}{cc}
2 & 0 \\
3 / 2 & 1 / 2
\end{array}\right)
\end{array}
$$

If $A=\left(\begin{array}{ll}a & b \\ c & d\end{array}\right)$ and $I=\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)$ show that $\mathbf{A}^{2}-(\mathbf{a}+\mathbf{d}) \mathbf{A}=(\mathbf{b c}-\mathbf{a d}) \mathbf{I}_{\mathbf{2}}$.

$$
\text { Solution: } \quad A^{2}=A \cdot A=\left(\begin{array}{ll}
a & b \\
c & d
\end{array}\right)\left(\begin{array}{ll}
a & b \\
c & d
\end{array}\right)=\left(\begin{array}{ll}
a^{2}+b c & a b+b d \\
a c+c d & b c+d^{2}
\end{array}\right) \text { and }(a+d) A=\left(\begin{array}{ll}
a^{2}+a d & a b+b d \\
c a+c d & a d+d^{2}
\end{array}\right)
$$

$$
A^{2}-(a+d) A=\left(\begin{array}{ll}
a^{2}+b c & a b+b d \\
a c+c d & b c+d^{2}
\end{array}\right)-\left(\begin{array}{cc}
a^{2}+a d & a b+b d \\
c a+c d & a d+d^{2}
\end{array}\right)=\left(\begin{array}{cc}
b c-a d & 0 \\
0 & b c-a d
\end{array}\right)=(b c-a d)\left(\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right)
$$

$=(b c-a d) \mathbf{I}_{2}$.

$$
\text { If } A=\left(\begin{array}{lll}
5 & 2 & 9 \\
1 & 2 & 8
\end{array}\right), B=\left(\begin{array}{cc}
1 & 7 \\
1 & 2 \\
5 & -1
\end{array}\right) \text { verify } \quad \text { that }(\mathbf{A B})^{\mathrm{T}}=\mathbf{B}^{\mathrm{T}} \mathbf{A}^{\mathrm{T}}
$$

$$
\text { Solution : } A B=\left(\begin{array}{lll}
5 & 2 & 9 \\
1 & 2 & 8
\end{array}\right)\left(\begin{array}{cc}
1 & 7 \\
1 & 2 \\
5 & -1
\end{array}\right)=\left(\begin{array}{l}
\begin{array}{l}
529 \\
\\
128
\end{array} \left\lvert\, \begin{array}{ll}
1 & 529 \\
1 & \\
5 & 12 \\
\hline
\end{array} \frac{7}{2}\right. \\
\hline
\end{array}\right.
$$

$$
\therefore(A B)^{T}=\left(\begin{array}{cc}
52 & 43  \tag{1}\\
30 & 3
\end{array}\right)
$$

$$
A^{T}=\left(\begin{array}{ll}
5 & 1 \\
2 & 2 \\
9 & 8
\end{array}\right) \text { and } B^{T}=\left(\begin{array}{ccc}
1 & 1 & 5 \\
7 & 2 & -1
\end{array}\right)
$$


$\therefore$ From (1) \& (2), (AB) $)^{T}=B^{T} A^{T}$
If $A=\left(\begin{array}{cc}3 & 1 \\ -1 & 2\end{array}\right)$ show that $A^{2}-5 A+7 I_{2}=0$
A ZAYAAN ABDUL M.SC. E, EDD.
JAYANIKONDAM,ARIYAIUR DT.
Solution: If $A=\left(\begin{array}{ll}a & b \\ c & d\end{array}\right)$ and $I=\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right) \mathbf{A}^{2}-(\mathbf{a}+\mathbf{d}) \mathbf{A}=(\mathbf{b c}-\mathbf{a d}) \mathbf{I}_{2}$.

$$
A=\left(\begin{array}{ll}
a & b \\
c & d
\end{array}\right)=\left(\begin{array}{cc}
3 & 1 \\
-1 & 2
\end{array}\right)
$$

$\therefore \mathbf{A}^{2}-(3+2) \mathbf{A}=((1)(-1)-(3)(2)) \mathbf{I}_{2}$ $\therefore A^{2}-5 A+7 I_{2}$

$$
\begin{aligned}
& \text { If } A=\left(\begin{array}{ccc}
1 & 2 & 1 \\
2 & -1 & 1
\end{array}\right) \text { and } B=\left(\begin{array}{cc}
2 & -1 \\
-1 & 4 \\
0 & 2
\end{array}\right) \text { show that }(\mathrm{AB})^{\mathrm{T}}=\mathrm{B}^{\mathrm{T}} \mathrm{~A}^{\mathrm{T}} \text {. } \\
& \text { Solution : }
\end{aligned}
$$

$$
\begin{align*}
& B^{T}=\left(\begin{array}{ccc}
2 & -1 & 0 \\
-1 & 4 & 2
\end{array}\right), A^{T}=\left(\begin{array}{cc}
1 & 2 \\
2 & -1 \\
1 & 1
\end{array}\right) \\
& B^{T} A^{T}=\left(\begin{array}{ccc}
2 & -1 & 0 \\
-1 & 4 & 2
\end{array}\right)\left(\begin{array}{cc}
1 & 2 \\
2 & -1 \\
1 & 1
\end{array}\right)=\left(\begin{array}{ccc}
2-1 & 0 & 2-1
\end{array}\right)  \tag{2}\\
& \begin{array}{c}
\text { From (1) and (2), }(\mathrm{AB})^{\mathrm{T}}=\mathrm{B}^{\mathrm{T}} \mathbf{A}^{\mathrm{T}} \text {. Hence } \\
\text { Let } A=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right), B=\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right) \text {, Show that } \quad(\mathbf{A}-\mathbf{B})^{\mathrm{T}}=\mathbf{A}^{\mathrm{T}}-\mathbf{B}^{\mathrm{T}}
\end{array} \\
& \text { Solution : }(\mathbf{A}-\mathbf{B})=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right)-\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right)=\left(\begin{array}{cc}
-3 & 2 \\
0 & -2
\end{array}\right) \quad \therefore(A-B)^{T}=\left(\begin{array}{cc}
-3 & 0 \\
2 & -2
\end{array}\right) \ldots \ldots . . \text { (1) } \\
& \mathrm{A}^{\mathrm{T}}=\left(\begin{array}{ll}
1 & 1 \\
2 & 3
\end{array}\right), B^{T}=\left(\begin{array}{ll}
4 & 1 \\
0 & 5
\end{array}\right) \quad \therefore \mathrm{A}^{\mathrm{T}}-B^{T}=\left(\begin{array}{ll}
1 & 1 \\
2 & 3
\end{array}\right)-\left(\begin{array}{ll}
4 & 1 \\
0 & 5
\end{array}\right)=\left(\begin{array}{cc}
-3 & 0 \\
2 & -2
\end{array}\right) \ldots \ldots . . \text { (2) } \\
& \therefore \text { From (1) \& (2) } \quad(A-B)^{T}=A^{T}-B^{T} \\
& \text { If } A=\left(\begin{array}{ccc}
4 & 3 & 1 \\
2 & 3 & -8 \\
1 & 0 & -4
\end{array}\right), B=\left(\begin{array}{ccc}
2 & 3 & 4 \\
1 & 9 & 2 \\
-7 & 1 & -1
\end{array}\right) \text { and } C=\left(\begin{array}{ccc}
8 & 3 & 4 \\
1 & -2 & 3 \\
2 & 4 & -1
\end{array}\right) \text { then verify that } \mathbf{A}+(\mathbf{B}+\mathbf{C})=(\mathbf{A}+\mathbf{B})+\mathbf{C} \\
& \text { Solution : } \\
& B+C=\left(\begin{array}{ccc}
10 & 6 & 8 \\
2 & 7 & 5 \\
-5 & 5 & -2
\end{array}\right) \\
& A+(B+C)=\left(\begin{array}{ccc}
4 & 3 & 1 \\
2 & 3 & -8 \\
1 & 0 & -4
\end{array}\right)+\left(\begin{array}{ccc}
10 & 6 & 8 \\
2 & 7 & 5 \\
-5 & 5 & -2
\end{array}\right)=\left(\begin{array}{ccc}
14 & 9 & 9 \\
4 & 10 & -3 \\
-4 & 5 & -6
\end{array}\right) \ldots(1) \\
& A+B=\left(\begin{array}{ccc}
6 & 6 & 5 \\
3 & 12 & -6 \\
-6 & 1 & -5
\end{array}\right) \\
& \therefore(A+B)+C=\left(\begin{array}{ccc}
6 & 6 & 5 \\
3 & 12 & -6 \\
-6 & 1 & -5
\end{array}\right)+\left(\begin{array}{ccc}
8 & 3 & 4 \\
1 & -2 & 3 \\
2 & 4 & -1
\end{array}\right)=\left(\begin{array}{ccc}
14 & 9 & 9 \\
4 & 10 & -3 \\
-4 & 5 & -6
\end{array}\right) \tag{2}
\end{align*}
$$

$$
\begin{aligned}
& \text { Let } A=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right), B=\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right), C=\left(\begin{array}{ll}
2 & 0 \\
1 & 2
\end{array}\right) \text { Show that } \quad \mathbf{A}(\mathbf{B C})=(\mathbf{A B}) \mathbf{C} \\
& \text { Solution : } A=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right), B=\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right), C=\left(\begin{array}{ll}
2 & 0 \\
1 & 2
\end{array}\right) \\
& B C=\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right)\left(\begin{array}{ll}
2 & 0 \\
1 & 2
\end{array}\right)=\left(\begin{array}{llll}
\hline & 0 & 2 & 4 \\
& & 0 & 0 \\
1 & 5 & 1 & 1
\end{array} 5_{2}^{2}\right)=\left(\begin{array}{ll}
8+0 & 0+0 \\
2+5 & 0+10
\end{array}\right)=\left(\begin{array}{cc}
8 & 0 \\
7 & 10
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
& A B=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right)\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right)=\left(\begin{array}{lllll}
1 & 2 & 1 & 1 & 2 \\
& & 4 & 0 \\
1 & 3 & 1 & 1 & 3 \\
5 \\
& 4 & & & 0 \\
1
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
& \text { Let } A=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right), B=\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right), C=\left(\begin{array}{ll}
2 & 0 \\
1 & 2
\end{array}\right) \text { Show that }(\mathbf{A}-\mathbf{B}) \mathbf{C}=\mathbf{A C}-\mathbf{B C} \\
& \text { Solution: } A=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right), B=\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right), C=\left(\begin{array}{ll}
2 & 0 \\
1 & 2
\end{array}\right) \\
& (A-B)=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right)-\left(\begin{array}{ll}
4 & 0 \\
1 & 5
\end{array}\right)=\left(\begin{array}{cc}
-3 & 2 \\
0 & -2
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
& A C=\left(\begin{array}{ll}
1 & 2 \\
1 & 3
\end{array}\right)\left(\begin{array}{ll}
2 & 0 \\
1 & 2
\end{array}\right)=\left(\begin{array}{lllll}
1 & 2 & 2 & 1 & 2 \\
& & 2 & & 0 \\
1 & 1 & 1 & 1 & 2 \\
\hdashline & 2 & 2 & & 0 \\
2 & 1 & & & 0
\end{array}\right)=\left(\begin{array}{ll}
2+2 & 0+4 \\
2+3 & 0+6
\end{array}\right)=\left(\begin{array}{ll}
4 & 4 \\
5 & 6
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
& \begin{array}{c}
\therefore A C-B C=\left(\begin{array}{ll}
4 & 4 \\
5 & 6
\end{array}\right)-\left(\begin{array}{cc}
8 & 0 \\
7 & 10
\end{array}\right)=\left(\begin{array}{cc}
-4 & 4 \\
-2 & -4
\end{array}\right) \ldots \ldots . . .(2) \\
\text { ( } \mathrm{A}-\mathrm{B}) \mathrm{C}=\mathrm{AC}-\mathrm{BC}
\end{array}
\end{aligned}
$$

. From (1) \& (2). $(\mathrm{A}-\mathrm{B}) \mathrm{C}=\mathrm{AC}-\mathrm{BC}$

Solve for $\mathbf{x}, \mathbf{y}\binom{x^{2}}{y^{2}}+2\binom{-2 x}{y}=\binom{5}{8}$
Solution: $\binom{x^{2}}{y^{2}}+2\binom{-2 x}{y}=\binom{5}{8}$

$$
\begin{gathered}
\Rightarrow x^{2}-4 x=5 \\
\Rightarrow \quad x=5,-1 \\
\Rightarrow \quad y^{2}-2 y=8 \\
\Rightarrow \therefore y=4, y=-2
\end{gathered}
$$

Given that $A=\left(\begin{array}{cc}1 & 3 \\ 5 & -1\end{array}\right), B=\left(\begin{array}{ccc}1 & -1 & 2 \\ 3 & 5 & 2\end{array}\right), C=\left(\begin{array}{ccc}1 & 3 & 2 \\ -4 & 1 & 3\end{array}\right)$ verify that $\mathbf{A}(\mathbf{B}+\mathbf{C})=\mathbf{A B}+\mathbf{A C}$

## Solution :

$$
\begin{aligned}
& A=\left(\begin{array}{cc}
1 & 3 \\
5 & -1
\end{array}\right), B=\left(\begin{array}{ccc}
1 & -1 & 2 \\
3 & 5 & 2
\end{array}\right), C=\left(\begin{array}{ccc}
1 & 3 & 2 \\
-4 & 1 & 3
\end{array}\right) \\
& (B+C)=\left(\begin{array}{ccc}
1 & -1 & 2 \\
3 & 5 & 2
\end{array}\right)+\left(\begin{array}{ccc}
1 & 3 & 2 \\
-4 & 1 & 3
\end{array}\right)=\left(\begin{array}{ccc}
2 & 2 & 4 \\
-1 & 6 & 5
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
& =\left(\begin{array}{ccc}
1+9 & -1+15 & 2+6 \\
5-3 & -5-5 & 10-2
\end{array}\right)=\left(\begin{array}{ccc}
10 & 14 & 8 \\
2 & -10 & 8
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{AB}+\mathrm{AC}=\left(\begin{array}{ccc}
10 & 14 & 8 \\
2 & -10 & 8
\end{array}\right)+\left(\begin{array}{ccc}
-11 & 6 & 11 \\
9 & 14 & 7
\end{array}\right)=\left(\begin{array}{ccc}
-1 & 20 & 19 \\
11 & 4 & 15
\end{array}\right) \ldots \ldots \ldots \ldots . .(2) \\
& \therefore \text { From (1) \& (2) } \quad \mathbf{A}(\mathbf{B}+\mathbf{C})=\mathbf{A B}+\mathbf{A C}
\end{aligned}
$$

If $A=\left(\begin{array}{lll}1 & -1 & 2\end{array}\right), B=\left(\begin{array}{cc}1 & -1 \\ 2 & 1 \\ 1 & 3\end{array}\right)$ and $C=\left(\begin{array}{cc}1 & 2 \\ 2 & -1\end{array}\right)$ show that $(\mathrm{AB}) \mathrm{C}=\mathrm{A}(\mathrm{BC})$.
Solution :

$$
\begin{aligned}
& (A B) C=\left(\begin{array}{ll}
1 & 4
\end{array}\right) \times\left(\begin{array}{cc}
1 & 2 \\
2 & -1
\end{array}\right)=\left(\begin{array}{lll}
14 & 14 & 1 \\
& & \\
2 & & 2 \\
-1
\end{array}\right)=\left(\begin{array}{lll}
1+8 & 2-4
\end{array}\right)=\left(\begin{array}{ll}
9 & -2
\end{array}\right) \ldots \ldots(1)
\end{aligned}
$$

$$
\begin{aligned}
& =(-1-4+14 \quad 3-3-2)=(9-2) \ldots \ldots \ldots \ldots . .(2)
\end{aligned}
$$

$$
\begin{aligned}
& \text { If } A=\left(\begin{array}{cc}
1 & 1 \\
-1 & 3
\end{array}\right), B=\left(\begin{array}{cc}
1 & 2 \\
-4 & 2
\end{array}\right), C=\left(\begin{array}{cc}
-7 & 6 \\
3 & 2
\end{array}\right) \text { verify that } \mathrm{A}(\mathrm{~B}+\mathrm{C})=\mathrm{AB}+\mathrm{AC} \text {. } \\
& \text { Solution: } \quad B+C=\left(\begin{array}{cc}
1 & 2 \\
-4 & 2
\end{array}\right)+\left(\begin{array}{cc}
-7 & 6 \\
3 & 2
\end{array}\right)=\left(\begin{array}{cc}
-6 & 8 \\
-1 & 4
\end{array}\right)
\end{aligned}
$$

$$
\begin{align*}
& A C=\left(\begin{array}{cc}
1 & 1 \\
-1 & 3
\end{array}\right) \times\left(\begin{array}{cc}
-7 & 6 \\
3 & 2
\end{array}\right)=\left(\begin{array}{cccc}
\begin{array}{ll}
1 & 1 \\
-7 & 1 \\
3 & 1
\end{array} & 6 \\
-1 & 3 & -1 & 2 \\
-7 & & 6 \\
3
\end{array}\right)=\left(\begin{array}{cc}
-7+3 & 6+2 \\
7+9 & -6+6
\end{array}\right)=\left(\begin{array}{ll}
-4 & 8 \\
16 & 0
\end{array}\right) \\
& A B+A C=\left(\begin{array}{cc}
-3 & 4 \\
-13 & 4
\end{array}\right)+\left(\begin{array}{cc}
-4 & 8 \\
16 & 0
\end{array}\right)=\left(\begin{array}{cc}
-7 & 12 \\
3 & 4
\end{array}\right) \tag{2}
\end{align*}
$$

From (1) and (2), $\mathrm{A}(\mathrm{B}+\mathrm{C})=\mathrm{AB}+\mathrm{AC}$.

## 4.GEOMETRY <br> 5 MARKS

Show that in a triangle, the medians are concurrent.
Solution : Themedians are the cevians where D, E, F are midpoints of BC, CA and AB
D is a mid point of $\frac{B D}{D C}=1 \ldots$ (1)
E is a midpoint of $\frac{C E}{E A}=1 \ldots$ (2)
F is a midpoint of $\frac{A F}{F B}=1 \ldots$ (3)
(1), (2) and (3) we get, $\frac{B D}{D C} \times \frac{C E}{E A} \times \frac{A F}{F B}=1 \times 1 \times 1=1$

Ceva's theorem is satisfied.
Ceva's theorem is satisfied.
Hence the Medians are concurrent.

$P$ and $Q$ are the mid-points of the sides $C A$ and $C B$ respectively of a $\triangle A B C$, right angled at $C$. Prove that $4\left(\mathrm{AQ}^{2}+\mathrm{BP}^{2}\right)=54 \mathrm{AB}^{2}$.
Solution :
$\triangle \mathrm{AQC}$ is a right triangle at $\mathrm{C}, \Rightarrow \mathrm{AQ}^{2}=\mathrm{AC}^{2}+\mathrm{QC}^{2} \ldots \ldots .$. (1)
$\triangle \mathrm{BPC}$ is a right triangle at $\mathrm{C}, \Rightarrow \mathrm{BP}^{2}=\mathrm{BC}^{2}+\mathrm{CP}^{2} \ldots$. (2)
From (1) and (2), $\mathrm{AQ}^{2}+\mathrm{BP}^{2}=\mathrm{AC}^{2}+\mathrm{QC}^{2}+\mathrm{BC}^{2}+\mathrm{CP}^{2}$

$4\left(\mathrm{AQ}^{2}+\mathrm{BP}^{2}\right)=4 \mathrm{AC}^{2}+4 \mathrm{QC}^{2}+4 \mathrm{BC}^{2}+4 \mathrm{CP}^{2}=5 \mathrm{AB}^{2}$ (By Pythagoras Theorem)
In $\triangle \mathrm{ABC}$ if $\mathrm{DE} \| \mathrm{BC}, \mathrm{AD}=8 \mathrm{x}-7, \mathrm{DB}=5 \mathrm{x}-3, \mathrm{AE}=4 \mathrm{x}-3$ and $\mathrm{EC}=3 \mathrm{x}-1$, find the value of x .
Solution : Given $\mathrm{AD}=8 \mathrm{x}-7, \mathrm{DB}=5 \mathrm{x}-3, \mathrm{AE}=4 \mathrm{x}-3$ and $\mathrm{EC}=3 \mathrm{x}-1$
$\mathrm{DE} \| \mathrm{BC}$, By Thales theorem

$$
\begin{gathered}
\frac{A D}{D B}=\frac{A E}{E C} \\
\frac{8 x-7}{5 x-3}=\frac{4 x-3}{3 x-1}
\end{gathered}
$$



## Statement and prove Angle Bisector Theorem

Statement The internal bisector of an angle of a tri angle divides the opposite side internally in the ratio of the corresponding sides containing the angle.
Given : In $\triangle \mathrm{ABC}, \mathrm{AD}$ is the internal bisector
To Prove : $\frac{A B}{A C}=\frac{B D}{C D}$
Construction : Draw CE parallel to AB. Extend AD to E
Proof : In $\triangle \mathrm{ABD} \sim \triangle \mathrm{ECD}, A B \| \mathrm{CE}$
$\angle \mathrm{AEC}=\angle \mathrm{BAE} \quad$ Altemate angles equal.


In $\triangle \mathrm{ACE}$ is isosceles
$\angle \mathrm{CAE}=\angle \mathrm{CEA}, \quad \mathrm{AC}=\mathrm{CE} . .$. (1)
By AA Similarity $\quad \triangle \mathrm{ABD} \sim \triangle \mathrm{ECD}$

$$
\begin{aligned}
& \frac{\mathrm{AB}}{\mathrm{CE}}=\frac{\mathrm{BD}}{\mathrm{CD}} \\
\Rightarrow & \frac{\mathrm{AB}}{\mathrm{AC}}=\frac{\mathrm{BD}}{\mathrm{CD}}
\end{aligned}
$$

Hence proved.

## Statement and prove Basic Proportionality Theorem or Thales theorem

## Statement

A straight line drawn parallel to a side of triangle intersecting the other two sides, divides the sides in the same ratio.
Given: In $\triangle \mathrm{ABC}, \mathrm{D}$ is a point on AB and E is a point on AC
To Prove : $\frac{A D}{D B}=\frac{A E}{E C}$
Construction : Draw a line DE\|BC


Proof: In $\triangle \mathrm{ADE}$ and $\triangle \mathrm{ABC}, \mathrm{DE} \| \mathrm{BC}$

$$
\angle \mathrm{A} \text { common angle }
$$

$\angle \mathrm{ADE}=\angle \mathrm{ABC} \quad$ Corresponding angles are equal

$$
\text { By AA similarity } \quad \triangle \mathrm{ADE} \sim \triangle \mathrm{ABC}
$$

$$
\frac{\mathrm{AD}}{\mathrm{AD}+\mathrm{DB}}=\frac{\mathrm{AE}}{\mathrm{AE}+\mathrm{EC}}
$$

$$
\begin{aligned}
& \frac{A D}{A D}+\frac{A D}{D B}=\frac{A E}{A E}+\frac{A E}{E C} \\
& 1+\frac{A D}{D B}=1+\frac{A E}{E C} \quad \begin{array}{l}
\Rightarrow \frac{A D}{D B}=\frac{A E}{E C} \\
\text { Hence proved }
\end{array}
\end{aligned}
$$

## Statement and prove Pythagoras Theorem

Statement
In a right angle triangle, the square on the hypotenuse is equal to the sum of the squares on the other two sides.
Given : In $\triangle \mathrm{ABC}, \mathrm{A}=90^{\circ}$
To prove : $\mathrm{AB}^{2}+\mathrm{AC}^{2}=\mathrm{BC}^{2}$
Construction : Draw $\mathrm{AD} \perp \mathrm{BC}$
Proof : In $\triangle \mathrm{ABC}$ and $\triangle \mathrm{ABD}$

$$
\begin{aligned}
& \angle \mathrm{B} \text { is common } \\
& \angle \mathrm{BAC}=\angle \mathrm{BDA}=90^{\circ}
\end{aligned}
$$

$\triangle \mathrm{ABC} \sim \triangle \mathrm{ABD}$

$$
\frac{\mathrm{AB}}{\mathrm{BD}}=\frac{\mathrm{BC}}{\mathrm{AB}} \Rightarrow \mathrm{AB}^{2}=\mathrm{BC} \times \mathrm{BD}
$$

In $\triangle A B C$ and $\triangle A D C$
$\angle \mathrm{C}$ is common $\angle \mathrm{BAC}=\angle \mathrm{ADC}=90^{\circ}$


By AA similarity,

$$
\begin{equation*}
\Delta \mathrm{ABC} \sim \Delta \mathrm{ADC} \quad \frac{\mathrm{BC}}{\mathrm{AC}}=\frac{\mathrm{AC}}{\mathrm{DC}} \Rightarrow \mathrm{AC}^{2}=\mathrm{BC} \times \mathrm{DC} \ldots . \tag{2}
\end{equation*}
$$

Adding, (1) and (2) $\mathrm{AB}^{2}+\mathrm{AC}^{2}=\mathrm{BC} \times \mathrm{BD}+\mathrm{BC} \times \mathrm{DC}=\mathrm{BC}(\mathrm{BD}+\mathrm{DC})=\mathrm{BC} \times \mathrm{BC}=\mathrm{BC}^{2}$
Hence proved

## 5 MARKS

5. COORDINATE GEOMETRY

Find the equation of the perpendicular bisector of the line joining the points $A(-4,2)$ and $B(6,-4)$ Solution :
: D is the midpoint of $\mathrm{AB} \quad \therefore \mathrm{D}=\left(\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right)=\left(\frac{-4+6}{2}, \frac{2-4}{2}\right)=(1,-1)$

$$
\text { Slope of } \mathrm{AB}=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{(-4)-(2)}{(6)-(-4)}=\frac{-4-2}{6+4}=\frac{-6}{10}=\frac{-3}{5}
$$

$$
\therefore \text { Slope of } \mathrm{CD}=\frac{5}{3}(\because \mathrm{CD} \perp \mathrm{AB})
$$


$\therefore$ Equation of perpendicular bisector CD is $\Rightarrow \mathrm{y}-\mathrm{y}_{1}=\mathrm{m}\left(\mathrm{x}-\mathrm{x}_{1}\right) \quad$ here $\mathrm{m}=\frac{5}{3} \quad, \quad\left(x_{1}, y_{1}\right)=(1,-1)$

$$
y+1=\frac{5}{3}(x-1) \Rightarrow 3 y+3=5 x-5 \Rightarrow 5 x-3 y-8=0
$$

Find the area of the quadrilateral whose vertices are $(-9,0),(-8,6),(-1,-2)$ and $(-6,-3)$ Solution :

Area of quadrilateral

$$
\begin{aligned}
& =\frac{1}{2} \\
& =\frac{1}{2}\left[\begin{array}{cccc}
-8 & -9 & -6 & -1 \\
6 & 0 & -3 & -2 \\
y_{1}
\end{array}\right] \\
& =\frac{1}{2}[(0+27+12-6)-(-54+0+3+16)] \\
& =\frac{1}{2}[33-(-35)]=\frac{1}{2}[68]=34 \text { sq. units }
\end{aligned}
$$

Find the area of the quadrilateral whose vertices are $(-9,0),(-8,6),(-1,-2)$ and $(-6,-3)$
Solution :
Area of quadrilateral

$$
\begin{aligned}
& =\frac{1}{2} \\
& =\frac{1}{2}[(0+27+12-6)-(-54+0+3+16)] \\
& =\frac{1}{2}[33-(-35)]=\frac{1}{2}[68]=34 \text { sq. units }
\end{aligned}
$$

Find the area of the quadrilateral whose vertices are $(-9,-2),(-8,-4),(2,2)$ and $(1,-3)$ Solution:

$$
\begin{aligned}
\text { Area of quadrilateral } & =\frac{1}{2}\left\{\begin{aligned}
x_{1} & \frac{1}{2}\left[\begin{array}{cccc}
-9 & -8 & 1 & 2 \\
-2 & -4 & -3 & 2
\end{array}\right] \\
& =\frac{1}{2}[(36+24+2-4)-(16-4-6-18)] \\
& =\frac{1}{2}[58-(-12)]=\frac{1}{2}[70]=35 \text { sq. units }
\end{aligned}\right\}
\end{aligned}
$$

Prove analytically that the line segment joining the mid-points of two sides of a triangle is parallel to the third side and is equal to half of its length.
Solution :

$$
\begin{aligned}
& \qquad \begin{array}{l}
S=\left(\frac{a+c}{2}, \frac{b+d}{2}\right) \text { and } \mathrm{T}=\left(\frac{a+e}{2}, \frac{b+f}{2}\right) \\
\text { slope of } \mathrm{ST} \\
=\frac{f-d}{e-c} \quad \text { and } \quad \text { slope of } \mathrm{QR}=\frac{f-d}{e-c}
\end{array} \quad \therefore \mathrm{ST} \text { is parallel to } \mathrm{QR} . \\
& \qquad \begin{aligned}
& \mathrm{ST}=\sqrt{\left(\frac{a+e}{2}-\frac{a+c}{2}\right)^{2}+\left(\frac{b+f}{2}-\frac{b+d}{2}\right)^{2}} \\
&=\frac{1}{2} \sqrt{(e-c)^{2}+(f-d)^{2}} \quad \mathrm{ST}=\frac{1}{2} Q R \\
& \text { JUZAYAAN ABDUL }
\end{aligned}
\end{aligned}
$$

## A ZAYAAN ABDUL M.SC, BED. A ZAYAAN ABDUL M.SC,

The given diagram shows a plan for constructing a new parking lot at a campus. It is estimated that such construction would cost $₹ 1300$ per square feet. What will be the total cost for making the parking lot?

Solution :

Area of parking lot $=\frac{1}{2}$ ?

$$
\begin{aligned}
& =\frac{1}{2}\left\{\begin{array}{l}
2 \\
2
\end{array}\right. \\
& =\frac{1}{2}\{(10+45+28+2)-(10+20+9+14)\} \\
& =\frac{1}{2}\{85-53\}=\frac{1}{2}(32)=16 \text { sq. units. }
\end{aligned}
$$



Total cost for constructing the parking lot $=16 \times 1300=\mathbf{~} 20800$
A triangular shaped glass with vertices at $\mathbf{A}(-5,-4), \mathrm{B}(1,6)$ and $\mathrm{C}(7,-4)$ has to be painted. If one bucket of paint covers 6 square feet, how many buckets of paint will be required to paint the whole glass, if only one coat of paint is applied.
Solution :
$\therefore$ Area of triangle $=$


$$
\begin{aligned}
& =\frac{1}{2}\left[\begin{array}{cccc}
-5 & 1 & 7 & -5 \\
-4 & 6 & -4 & -4
\end{array}\right] \\
& =\frac{1}{2}[(-30-4-28)-(-4+42+20)]=\frac{1}{2}[-120]=60 \text { sq. units }
\end{aligned}
$$

$\therefore$ No. of paint cans needed $=\frac{60}{6}=10$
Find the area of a triangle formed by the lines $3 x+y-2=0,5 x+2 y-3=0$ and $2 x-y-3=0$.
Solution: $3 x+y-2=0$

$$
\begin{align*}
& 5 x+2 y-3=0  \tag{1}\\
& 2 x-y-3=0
\end{align*}
$$

(2) $\Rightarrow 5 \mathrm{x}+2 \mathrm{y}=3$

$$
\begin{aligned}
\left.\left.(3) \times 2 \Rightarrow \begin{array}{rl}
3 x+2 y & =3 \\
4 x-2 y & =6 \\
\hline 9 x \quad & =9 \\
x & =1
\end{array}\right) . \begin{array}{rl}
(2)
\end{array}\right)
\end{aligned}
$$

$$
\begin{aligned}
x & =1 \\
\therefore(3) \Rightarrow 2-y-3 & =0 \\
\Rightarrow \quad-y & =1
\end{aligned}
$$

$$
\Rightarrow \quad-y=1 \quad \therefore \quad y=-1
$$

$$
\therefore \mathrm{C} \text { is }(1,-1)
$$

Find the area of the quadrilateral whose vertices are $(-9,-2),(-8,-4),(2,2)$ and $(1,-3)$ Solution: Area of quadrilateral

$$
=\frac{1}{2}\left\{\begin{aligned}
x_{1}
\end{aligned} y_{y_{1}}^{x_{2}}\right\}=\frac{1}{2}\left[\begin{array}{ccccc}
-9 & -8 & 1 & 2 & -9 \\
-2 & -4 & -3 & 2 & -2
\end{array}\right]
$$



$$
=\frac{1}{2}[58-(-12)]=\frac{1}{2}[70]=35 \text { sq. units }
$$

$$
\begin{aligned}
& \text { (1) } \times 2 \Rightarrow 6 x+2 y=4 \\
& \text { (2) } \Rightarrow \frac{5 x+2 y=3}{x}=1 \\
& \text { Sub. in (1) } 3+y-2=0 \Rightarrow y=-1 \\
& \therefore \mathrm{~A}(1,-1) \\
& 3 x+y=2 \\
& \begin{array}{l}
2 x-y=3 \\
\hline 5 x=5
\end{array} \\
& \mathrm{x}=1 \quad \therefore \mathrm{y}=-1 \\
& \therefore \mathrm{~B} \text { is }(1,-1)
\end{aligned}
$$

## 8. STATISTICS AND PROBABILITY

## 5 MARKS

Find the mean and variance of the first $n$ natural numbers.
Solution :

$$
\text { Mean } \bar{x}=\frac{\sum x_{i}}{n}=\frac{n(n+1)}{2 \times)_{n}}=\frac{n+1}{2}
$$

Variance $\sigma^{2}=\frac{\sum x_{i}^{2}}{n}-\left(\frac{\sum x_{i}}{n}\right)^{2}=\frac{n(n+1)(2 n+1)}{6 \times \eta}-\left[\frac{h(n+1)}{2 \times n}\right]^{2}$

$$
=\frac{(n+1)(2 n+1)}{6}-\left[\frac{n(n+1)}{2}\right]^{2}=\frac{n^{2}-1}{12}
$$

48 students were asked to write the total number of hours per week they spent on watching televi sion With this information find the standard deviation of hours spent for watching television.

\section*{| $x$ | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 3 | 6 | 9 | 13 | 8 | 5 | 4 |}

Solution

| $x$ | $f$ | $d=x-9$ | $d^{d}$ | $f \cdot d$ | $f \cdot f$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | 3 | -3 | 9 | -9 | 27 |
| 7 | 6 | -2 | 4 | -12 | 24 |
| 8 | 9 | -1 | 1 | -9 | 9 |
| 9 | 13 | 0 | 0 | 0 | 0 |
| 10 | 8 | 1 | 1 | 8 | 8 |
| 11 | 5 | 2 | 4 | 10 | 20 |
| 12 | 4 | 3 | 9 | 12 | 36 |
|  | 48 |  |  | 0 | 124 |

$$
\begin{aligned}
\sigma & =\sqrt{\frac{\sum f d^{2}}{\sum f}-\left(\frac{\sum f d}{\sum f}\right)^{2}} \\
& =\sqrt{\frac{124}{48}} \\
& =1.6
\end{aligned}
$$

## The marks scored by the students in a slip test are given below

| $\boldsymbol{x}$ | 4 | 6 | 8 |  | 0 | 12 | Find the standard deviation of |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f$ | 7 | 3 | 5 |  |  | 5 |  |
| Solution : |  |  |  |  |  |  |  |
| $x$ | $f$ | $d=x-8$ |  | $d^{2}$ | f.d | f..$^{2}$ |  |
| 4 | 7 | -4 |  | 16 | -28 | 112 |  |
| 6 | 3 | -2 |  | 4 | -6 | 12 | $\sqrt{\sum f d^{2}\left(\sum f d\right)^{2}}$ |
| 8 | 5 | 0 |  | 0 | 0 | 0 | $=\sqrt{\frac{\sum f d}{}} \frac{1}{}-\left(\frac{\sum f d}{\sum f}\right)$ |
| 10 | 9 | 2 |  | 4 | 18 | 36 |  |
| 12 | 5 | 4 |  | 16 | 20 | 80 | $=\sqrt{\frac{240}{29}-\left(\frac{4}{29}\right)^{2}}=2.87$ |
|  | 29 |  |  |  | 4 | 240 |  |
|  |  |  |  |  |  |  |  |

Three unbiased coins are tossed once. Find the probability of getting atmost 2 tails or atleast 2 heads Solution: $\mathrm{S}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{THH}),(\mathrm{HTT}),(\mathrm{THT}),(\mathrm{TTH}),(\mathrm{TTT})\} \quad \mathrm{n}(\mathrm{S})=8$
Let A - at most 2 tails

$$
\begin{aligned}
& \text { most } 2 \text { tails } \\
& \mathrm{A}=\{(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{THH}),(\mathrm{HTT}),(\mathrm{THT}),(\mathrm{TTH}),(\mathrm{HHH})\} \quad \mathrm{n}(\mathrm{~A})=7 \Rightarrow \mathrm{P}(\mathrm{~A})=\frac{7}{8}
\end{aligned}
$$

Let B - atleast 2 heads

$$
B=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{THH})\} \quad \mathrm{n}(\mathrm{~B})=4 \Rightarrow \mathrm{P}(\mathrm{~B})=\frac{4}{8}
$$

$\therefore \mathrm{A} \cap \mathrm{B}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{THH})\} \quad \mathrm{n}(\mathrm{A} \cap \mathrm{B})=4 \Rightarrow \mathrm{P}(\mathrm{A} \cap \mathrm{B})=\frac{4}{8}$

$$
\therefore \mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})-\mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\frac{7}{8}+\frac{4}{8}-\frac{4}{8}=\frac{7}{8} \quad \text { A ZAYAAN ABDUL M.SC.EBED. }
$$

A card is drawn from a pack of 52 cards. Find the probability of getting a king or a heart or a red card.
Solution : $\mathrm{n}(\mathrm{S})=52$
Let A king card, Let B heart card, Let C red card.
$P(A)=\frac{4}{52}, P(B)=\frac{13}{52}, P(C)=\frac{26}{52}, \quad \mathrm{P}(\mathrm{A} \cap \mathrm{C})=\frac{2}{52}, \mathrm{P}(\mathrm{A} \cap \mathrm{B})=\frac{1}{52}, \mathrm{P}(\mathrm{B} \cap \mathrm{C})=\frac{13}{52}$
$\mathrm{P}(\mathrm{A} \cap \mathrm{B} \cap \mathrm{C})=\frac{1}{52}$
$\mathrm{P}(\mathrm{A} \cup \mathrm{B} \cup \mathrm{C})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})+\mathrm{P}(\mathrm{C})-\mathrm{P}(\mathrm{A} \cap \mathrm{B})-\mathrm{P}(\mathrm{B} \cap \mathrm{C})-\mathrm{P}(\mathrm{C} \cap \mathrm{A})+\mathrm{P}(\mathrm{A} \cap \mathrm{B} \cap \mathrm{C})$

$$
=\frac{4}{52}+\frac{13}{52}+\frac{26}{52}-\frac{1}{52}-\frac{13}{52}-\frac{2}{52}+\frac{1}{52}=\frac{28}{52}=\frac{7}{13}
$$

A bag contains 5 red balls, 6 white balls, 7 green balls, 8 black balls. One ball is drawn at random from the bag. Find the probability that the ball drawn is (i) white (ii) black or red (iii) not white (iv) neither white nor black

Solution: $\mathrm{S}=\{5 \mathrm{R}, 6 \mathrm{~W}, 7 \mathrm{G}, 8 \mathrm{~B}\}$
i) Let A - White ball $\mathrm{n}(\mathrm{A})=6 \Rightarrow P(A)=\frac{6}{26}=\frac{3}{13}$
ii) Let B-Black (or) red $n(B)=5+8=13 \Rightarrow P(B)=\frac{13}{26}=\frac{1}{2}$
iii) Let C -not white $\mathrm{n}(\mathrm{C})=20 \Rightarrow P(C)=\frac{20}{26}=\frac{10}{13}$
iv) Let D - Neither white nor black $\mathrm{n}(\mathrm{D})=12 \Rightarrow P(D)=\frac{12}{26}=\frac{6}{13}$

What is the probability of drawing either a king or a queen in a single draw from a well shuffled pack of 52 cards?
Solution : Total number of cards $=52$
Let A king card $n(A)=4 \Rightarrow P(A)=\frac{4}{52}$
Let B queen card $n(B)=4 \Rightarrow P(B)=\frac{4}{52} \quad \therefore P(A \cap B)=\frac{0}{52}$

Marks of the students in a particular subject of a class are given below.

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | - |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{c}\text { Number of } \\ \text { students }\end{array}$ | 8 | 12 | 17 | 14 | 9 | 7 | 4 | - |

Solution :

| Marts | $\begin{array}{\|c} \begin{array}{c} \text { Mid } \\ \text { value } \\ (x) \end{array} \end{array}$ | $f$ | $\mathrm{d}=$ $\mathrm{x}-\mathrm{A}$ | $d=\frac{x-d}{c}$ | $f d$ | $f d^{2}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0-10$ | 5 | 8 | -30 | -3 | -24 | 72 |
| 10-20 | 15 | 12 | -20 | -2 | -24 | 48 |
| 20-30 | 25 | 17 | -10 | -1 | -17 | 17 |
| 30-40 | 35 | 14 | 0 | 0 | 0 | 0 |
| 40-50 | 45 | 9 | 10 | 1 | 9 | 9 |
| 50-60 | 55 | 7 | 20 | 2 | 14 | 28 |
| 60-70 | 65 | 4 | 30 | 3 | 12 | 36 |
|  |  | $\Sigma \mathrm{f}=71$ |  |  | Efd | $\underset{=210}{\sum \mathrm{fd}}$ |

$$
\text { Standard deviation } \begin{aligned}
\sigma & =c \times \sqrt{\frac{\sum f d^{2}}{\sum f}-\left(\frac{\sum f d}{\sum f}\right)^{2}} \\
\sigma & =10 \times \sqrt{\frac{210}{71}-\left(-\frac{30}{71}\right)^{2}} \\
& =16.67
\end{aligned}
$$

Two unbiased dice are rolled once. Find the probability of getting (i) a doublet (equal numbers on both dice) (ii) the product as a prime number (iii) the sum as a prime number (iv) the sum as 1
Solution: $\mathrm{S}=\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1),(2,2),(2,3),(2,4),(2,5),(2,6)$
$(3,1),(3,2),(3,3),(3,4),(3,5),(3,6),(4,1),(4,2),(4,3),(4,4),(4,5),(4,6)$
$(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5),(6,6)\}$
$n(S)=36$
i) $\quad \begin{aligned} & \text { Let A a doublet } \\ & \mathrm{A}=\{(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)\} \quad \mathrm{n}(\mathrm{A})=6 \quad \therefore P(A)=\frac{6}{36}=\frac{1}{6}\end{aligned}$

Let B the product as a prime number.
$\mathrm{B}=\{(1,2),(1,3),(1,5),(2,1),(3,1),(5,1)\} \quad \mathrm{n}(\mathrm{B})=6 \quad \therefore P(B)=\frac{6}{36}=\frac{1}{6}$
iii) Let C be the sum of numbers on the dice is prime.
$\mathrm{C}=\{(1,1),(1,2),(1,4),(1,6),(2,1),(2,3),(2,5),(3,2)$,

$$
(3,4),(4,1),(4,3),(5,2),(5,6),(6,1),(6,5)\} \quad \mathrm{n}(\mathrm{C})=15 \quad \therefore P(C)=\frac{15}{36}=\frac{5}{12}
$$

iv) Let $D$ be the sum of numbers is $1 . \quad n(D)=0 \quad \therefore P(D)=0$

If two dice are rolled, then find the prob ability of getting the product of face value $\mathbf{6}$ or the difference of face values 5 .
Solution: $\mathrm{S}=\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1),(2,2),(2,3),(2,4),(2,5),(2,6)$
(3,1),(3,2),(3,3),(3,4),(3,5),(3,6), (4,1),(4,2),(4,3),(4,4),(4,5),(4,6) $(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5),(6,6)\}$
Let A - Product of face value is $6 . \quad \therefore \mathrm{n}(\mathrm{S})=36$
$\mathrm{A}=\{(1,6),(2,3),(3,2),(6,1)\} \Rightarrow \mathrm{n}(\mathrm{A})=4 \Rightarrow \mathrm{P}(\mathrm{A})=\frac{4}{36}$
Let $B$ - Difference of face value is 5. $\quad B=\{(6,1)\} \Rightarrow n(B)=1 \Rightarrow P(B)=\frac{1}{36}$
$A \cap B=\{(6,1)\} \Rightarrow n(A \cap B)=1 \Rightarrow P(A \cap B)=\frac{1}{36}$
$\therefore \mathrm{P}(\mathrm{A} \cup \mathrm{B})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})-\mathrm{P}(\mathrm{A} \cap \mathrm{B})=\frac{4}{36}+\frac{1}{36}-\frac{1}{36}=\frac{4}{36}=\frac{1}{9}$
In a class of 50 students, 28 opted for NCC, 30 opted for NSS and 18 opted both NCC and NSS.
One of the students is selected at random. Find the probability that
(i) The student opted for NCC but not NSS. (ii) The student opted for NSS but not NCC.
(iii) The student opted for exactly one of them.

Solution: Let A and B be NCC and NSS

## A ZAYAAN ABDUL M.SC. ${ }^{\text {B }}$ EDD

Total number of students $n(S)=50$
$\mathrm{n}(\mathrm{A})=28, \mathrm{n}(\mathrm{B})=30, \mathrm{n}(\mathrm{A} \cap \mathrm{B})=18 \Rightarrow P(A)=\frac{28}{50}, P(B)=\frac{30}{50}$ and $P(A \cap B)=\frac{18}{50}$
(i) Probability of the students opted for NCC but not NSS $P(A \cap \bar{B})=P(A)-P(A \cap B)=\frac{28}{50}-\frac{18}{50}=\frac{1}{5}$
(ii) Probability of the students opted for NSS but not NCC. $\mathrm{P}(\mathrm{A} \cap \overline{\mathrm{B}})=\mathrm{P}(\mathrm{B})-\mathrm{P}(\mathrm{A} \cap \mathrm{B})=\frac{30}{50}-\frac{18}{50}=\frac{6}{25}$
(iii) Probability of the students opted for exactly one of them $\mathrm{P}(\mathrm{A} \cap \overline{\mathrm{B}})+\mathrm{P}(\overline{\mathrm{A}} \cap \mathrm{B})=\frac{1}{5}+\frac{6}{25}=\frac{11}{25}$

From a well-shuffled pack of 52 cards, a card is drawn at random. Find the prob-ability of it being either a red king or a black queen.
Solution: $\mathrm{n}(\mathrm{S})=52$

$$
\text { Let A-Red King } \mathrm{n}(\mathrm{~A})=2 \Rightarrow \mathrm{P}(\mathrm{~A})=\frac{2}{52}
$$

$$
\begin{aligned}
& \text { Let } B \text { - Black Queen } n(B)=2 \Rightarrow P(B)=\frac{2}{52} \\
& \quad n(A \cap B)=0 \Rightarrow P(A \cap B)=\frac{0}{52} \\
& \therefore P(A \cup B)=P(A)+P(B)-P(A \cap B)=\frac{2}{52}+\frac{2}{52}-\frac{0}{52}=\frac{4}{52}=\frac{1}{13}
\end{aligned}
$$

Two dice are rolled. Find the probability that the sum of outcomes is (i) equal to 4 (ii) greater than 10 (iii) less than 13
Solution: $S=\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1),(2,2),(2,3),(2,4),(2,5),(2,6)$

$$
(3,1),(3,2),(3,3),(3,4),(3,5),(3,6),(4,1),(4,2),(4,3),(4,4),(4,5),(4,6)
$$

$$
(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5),(6,6)
$$

$$
n(S)=36
$$

(i) Let A the sum of outcome values equal to 4 .

$$
\begin{aligned}
& \text { sum of outcome values equal to } 4 . \\
& \mathrm{A}=\{(1,3),(2,2),(3,1)\} ; \mathrm{n}(\mathrm{~A})=3 . \quad P(A)=\frac{3}{36}=\frac{1}{12}
\end{aligned}
$$

(ii)Let $B$ the sum of outcome values greater than 10 .

$$
\begin{gathered}
\mathrm{B}=\{(5,6),(6,5),(6,6)\} ; \mathrm{n}(\mathrm{~B})=3 \\
\mathrm{~B}=3(B)=\frac{3}{36}=\frac{1}{12} .
\end{gathered}
$$

(iii) Let C the sum of outcomes less than 13.
$\mathrm{n}(\mathrm{C})=\mathrm{n}(\mathrm{S})=36 \quad P(C)=\frac{36}{36}=1$

From a well shuffled pack of 52 cards, one card is drawn at random. Find the probability of get ting (i) red card (ii) heart card (iii) red king (iv) face card (v) number card
Solution: $n(S)=52$
(i) Let A red card. $\mathrm{n}(\mathrm{A})=26 \Rightarrow P(A)=\frac{26}{52}=\frac{1}{2}$
(ii) Let B heart card. $\mathrm{n}(\mathrm{B})=13 \Rightarrow P(B)=\frac{13}{52}=\frac{1}{4}$
(iii) Let C red king card. $\mathrm{n}(\mathrm{C})=2 \Rightarrow P(C)=\frac{2}{52}=\frac{1}{26}$

## A ZAYAAN ABDUL M. SC $_{2}$, BED. JAYANIKONDAM,ARIYALUR DT

(iv) Let D face card.

The face cards are Jack (J), Queen (Q), and King (K). $n(D)=4 \times 3=12 \Rightarrow P(D)=\frac{12}{52}=\frac{3}{13}$
(v) Let E a number card.
$\mathrm{E})=4 \times 9=36 \Rightarrow P(E)=\frac{36}{52}=\frac{9}{13}$
Three fair coins are tossed together. Find the probability of getting (i) all heads (ii) atleast one tail (iii) atmost one head (iv) atmost two tails

Solution : When 3 fair coins are tossed,
$\mathrm{S}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{HTT}),(\mathrm{THH}),(\mathrm{THT}),(\mathrm{TTH}),(\mathrm{TTT})\}$

$$
\therefore \mathrm{n}(\mathrm{~S})=8
$$

i) Let A all heads. $\mathrm{A}=\{(\mathrm{HHH})\} \quad \mathrm{n}(\mathrm{A})=1 \quad \therefore P(A)=\frac{1}{8}$
ii) Let B atleast one tail
$\mathrm{B}=\{(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{HTT}),(\mathrm{THH}),(\mathrm{THT}),(\mathrm{TTH}),(\mathrm{TTT})\} \quad \mathrm{n}(\mathrm{B})=7 \Rightarrow P(B)=\frac{7}{8}$
iii) Let C at most one head.
$\mathrm{C}=\{(\mathrm{HTT}),(\mathrm{THT}),(\mathrm{TTH}),(\mathrm{TTT})\} \quad \mathrm{n}(\mathrm{C})=4 \Rightarrow P(C)=\frac{4}{8}=\frac{1}{2}$
iv) Let D - atmost 2 tails
$\mathrm{D}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTT}),(\mathrm{HTH}),(\mathrm{THH}),(\mathrm{THT}),(\mathrm{TTH})\} \quad \mathrm{n}(\mathrm{D})=7 \Rightarrow P(D)=\frac{7}{8}$

The king and queen of diamonds, queen and jack of hearts, jack and king of spades are removed
from a deck of 52 playing cards and then well shuffled. Now one card is drawn at random from the re maining cards. Determine the probabil ity that the card is (i) a clavor (ii) a queen of red card (iii) a king of black card

Solution: By the data given, $n(S)=52-2-2-2=46$
i) Let A a clavor card. $\mathrm{n}(\mathrm{A})=13 \quad \Rightarrow \quad P(A)=\frac{13}{46}$
ii) Let $B$ - queen of red card. $n(B)=0 \Rightarrow P(B)=0 \quad$ (queen diamond and heart are included in $S$ )
iii) Let C - King of black cards $\mathrm{n}(\mathrm{C})=1$ (encluding spade king) $\Rightarrow P(C)=\frac{1}{46}$

Two dice are rolled together. Find the probability of getting a doublet or sum of faces as 4 .
Solution : $\mathrm{S}=\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1),(2,2),(2,3),(2,4),(2,5),(2,6)$ (3,1),(3,2),(3,3),(3,4),(3,5),(3,6), (4,1),(4,2),(4,3),(4,4),(4,5),(4,6) $(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5),(6,6)\} \quad n(S)=36$
Let A a double
Let A a doublet
$\mathrm{A}=\{(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)\} \quad \mathrm{n}(\mathrm{A})=6 \Rightarrow P(A)=\frac{6}{36}$
Let B face sum 4.
$\mathrm{~B}=\{(1,3),(2,2),(3,1)\} \quad \mathrm{n}(\mathrm{B})=3 \Rightarrow P(B)=\frac{3}{36}$
$\mathrm{A} \cap \mathrm{B}=\{(2,2)\} \Rightarrow \mathrm{n}(\mathrm{A} \cap \mathrm{B})=1 \Rightarrow P(A \cap B)=\frac{1}{36}$
$P(A \cup B)=P(A)+P(B)-P(A \cap B)=\frac{6}{36}+\frac{3}{36}-\frac{1}{36}=\frac{8}{36}=\frac{2}{9}$
A coin is tossed thrice. Find the probability of getting exactly two heads or atleast one tail or two consecutive heads.
Solution: $\mathrm{S}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{THH}),(\mathrm{TTH}),(\mathrm{THT}),(\mathrm{HTT}),(\mathrm{TTT})\}$
$\mathrm{n}(\mathrm{S})=8$
Let $A$ - exactly 2 heads, $A=\{(H H T),(H T H),(T H H)\} \quad n(A)=3 \Rightarrow P(A)=\frac{3}{8}$
Let $B$ - atleast one tail,$B=\{(H H T),(H T H),(T H H),(T T H),(T H T),(H T T),(T T T)\} n(B)=7 \Rightarrow P(B)=\frac{7}{8}$
Let C - Consecutively 2 heads, $\mathrm{C}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{THH})\} \quad \mathrm{n}(\mathrm{C})=3 \Rightarrow \mathrm{P}(\mathrm{C})=\frac{3}{8}$

$$
A \cap B=\{(H H T),(H T H),(T H H)\}, n(A \cap B)=3 \Rightarrow P(A \cap B)=\frac{3}{8}
$$

$\mathrm{B} \cap \mathrm{C}=\{(\mathrm{HHT}),(\mathrm{THH})\}, \quad \mathrm{n}(\mathrm{B} \cap \mathrm{C})=2 \quad \Rightarrow \mathrm{P}(\mathrm{B} \cap \mathrm{C})=\frac{2}{8}$
$\mathrm{C} \cap \mathrm{A}=\{(\mathrm{HHT}),(\mathrm{THH})\}$,
$n(C \cap A)=2 \quad \Rightarrow P(C \cap A)=\frac{2}{8}$
$\mathrm{P}(\mathrm{A} \cup \mathrm{B} \cup \mathrm{C})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})+\mathrm{P}(\mathrm{C})-\mathrm{P}(\mathrm{A} \cap \mathrm{B})-\mathrm{P}(\mathrm{B} \cap \mathrm{C})-\mathrm{P}(\mathrm{C} \cap \mathrm{A})+\mathrm{P}(\mathrm{A} \cap \mathrm{B} \cap \mathrm{C})$

$$
=\frac{3}{8}+\frac{7}{8}+\frac{3}{8}-\frac{3}{8}-\frac{2}{8}-\frac{2}{8}+\frac{2}{8}=\frac{8}{8}=1
$$

A ZAYAAN ABDUL M.BC.E.ED
JAYANIGONDAM,ARYMIUR DT.

In a town of $\mathbf{8 0 0 0}$ people, $\mathbf{1 3 0 0}$ are over 50 years and $\mathbf{3 0 0 0}$ are females. It is known that $\mathbf{3 0 \%}$ of the females are over 50 years. What is the probability that a chosen individual from the town is either a female or over 50 years?
Solution: Let A-Female , B - Over 50 years

$$
\begin{aligned}
& \text { Let A - Female, B - Over } 50 \text { years } \\
& n(S)=8000, n(A)=3000, n(B)=1300 \quad n(A \cap B)=\frac{30}{100} \times 3000=900
\end{aligned}
$$

$$
\therefore \mathrm{P}(\mathrm{~A})=\frac{3000}{8000}, \mathrm{P}(\mathrm{~B})=\frac{1300}{8000}, \mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\frac{900}{8000}
$$

$$
P(A \cup B)=P(A)+P(B)-P(A \cap B)=\frac{3000+1300-900}{8000}=\frac{3400}{8000}=\frac{34}{80}=\frac{17}{40}
$$

Two dice are rolled once. Find the probability of getting an even number on the first die or a total of face sum 8 .
Solution: $\mathrm{S}=\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1),(2,2),(2,3),(2,4),(2,5),(2,6)$
(3,1),(3,2),(3,3),(3,4),(3,5),(3,6), (4,1),(4,2), (4,3), (4,4),(4,5),(4,6) $(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5),(6,6)\}$

$$
n(S)=36
$$

Let $A$ even number on the $1^{\text {" }}$ die
$A=\{(2,1),(2,2),(2,3),(2,4),(2,5),(2,6),(4,1),(4,2),(4,3),(4,4),(4,5),(4,6),(6,1),(6,2),(6,3),(6,4)$,

$$
(6,5),(6,6)\} \quad \mathrm{n}(\mathrm{~A})=18 \quad \Rightarrow \mathrm{P}(\mathrm{~A})=\frac{18}{36}
$$

$$
\begin{aligned}
& \text { Let } B \text { - Total of face sum as } 8 . \\
& \qquad B=\{(2,6),(3,5),(4,4),(5,3),(6,2)\} \quad n(B)=5 \quad \Rightarrow P(B)=\frac{5}{36}
\end{aligned}
$$

$$
\begin{aligned}
\mathrm{A} \cap \mathrm{~B}=\{(2,6),(4,4),(6,2)\} \quad \mathrm{n}(\mathrm{~A} \cap \mathrm{~B})=3 & \Rightarrow \mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\frac{3}{36} \\
\therefore \mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})-\mathrm{P}(\mathrm{~A} \cap \mathrm{~B}) & =\frac{18}{36}+\frac{5}{36}-\frac{3}{36}=\frac{20}{36}=\frac{5}{9}
\end{aligned}
$$

The King, Queen and Jack of the suit spade are removed from a deck of 52 cards. One card is selected from the remaining cards. Find the probability of getting (i) a diamond (ii) a queen (iii) a spade (iv) a heart card bearing the number 5 .

Solution : $\mathrm{n}(\mathrm{S})=52-3=49$
i) Let A - a diamond card $\mathrm{n}(\mathrm{A})=13 \quad \therefore P(A)=\frac{13}{49}$
ii) Let $B$ - a queen card $n(B)=3$ (except spade queen out of 4) $\quad \therefore P(B)=\frac{3}{49}$
iii) Let C - a spade card $\mathrm{n}(\mathrm{C})=10(13-3=10) \quad \therefore P(C)=\frac{10}{49}$
iv) Let $\mathrm{D}-5$ of heart $\quad \mathrm{n}(\mathrm{D})=1 \quad \therefore P(D)=\frac{1}{49}$

A box contains cards numbered $3,5,7,9, \ldots 35,37$. A card is drawn at random from the box. Find the probability that the drawn card have either multiples of 7 or a prime number.
Solution : $\mathrm{S}=\{3,5,7,9, \ldots . . . . . . .35,37\} \Rightarrow \mathrm{n}(\mathrm{S})=18$
Let A -multiple of 7. $\mathrm{A}=\{7,14,21,28,35\} \quad \mathrm{n}(\mathrm{A})=5 \Rightarrow \mathrm{P}(\mathrm{A})=\frac{5}{18}$
Let B - a prime number

$$
\begin{aligned}
& \mathrm{B} \text { - a prime number } \\
& \mathrm{B}=\{3,5,7,11,13,17,19,23,29,31,37\} \quad \mathrm{n}(\mathrm{~B})=11 \Rightarrow \mathrm{P}(\mathrm{~B})=\frac{11}{18}
\end{aligned}
$$

$$
\mathrm{A} \cap \mathrm{~B}=\{7\} \quad \mathrm{n}(\mathrm{~A} \cap \mathrm{~B})=1 \Rightarrow \mathrm{P}(\mathrm{~A} \cap \mathrm{~B})=\frac{1}{18}
$$

$$
\therefore \mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\mathrm{P}(\mathrm{~A})+\mathrm{P}(\mathrm{~B})-\mathrm{P}(\mathrm{~A} \cup \mathrm{~B})=\frac{5}{18}+\frac{11}{18}-\frac{1}{18}=\frac{15}{18}=\frac{5}{6}
$$

Find the variance and standard deviation of the wages of 9 workers given below:
₹310, ₹290, ₹320, ₹280, ₹300, ₹290, ₹320, ₹310, ₹280.

Solution : | $x$ | $d=x-300$ | $d^{2}$ |
| :---: | :---: | :---: |
|  | 280 | -20 |
| 400 | -20 | 400 |
|  | 280 | -10 |
| 290 | 100 |  |
| 290 | -10 | 100 |
| 300 | 0 | 0 |
| 310 | 10 | 100 |
| 310 | 10 | 100 |
|  | 320 | 20 |
| 320 | 20 | 400 |
|  |  | $\Sigma \mathrm{~d}-0$ |
|  | $\Sigma d^{2}=2000$ |  |

$$
\begin{aligned}
& \begin{aligned}
\text { variance } & \sigma^{2}=\frac{\sum d^{2}}{n}-\left(\frac{\sum d}{n}\right)^{2} \\
& =\frac{2000}{9}-\left(\frac{0}{9}\right)^{2} \\
& =\frac{2000}{9}=222.2
\end{aligned} \\
& \text { S.D }= \sqrt{222.2}=14.91
\end{aligned}
$$

Find the coefficient of variation of $\mathbf{2 4}, 26,33,37,29,31$.
Solution: Given data is $24,26,33,37,29,31 . \quad \bar{x}=\frac{24+26+33+37+29+31}{6}=\frac{180}{6}=30$

| $x$ | $\mathrm{~d}=x-30$ | $\mathrm{~d}^{2}$ |
| :---: | :---: | :---: |
| 24 | -6 | 36 |
| 26 | -4 | 16 |
| 29 | -1 | 1 |
| 31 | 1 | 1 |
| 33 | 3 | 9 |
| 37 | 7 | 49 |
|  | 0 | 112 |

$$
\begin{aligned}
& \therefore \sigma=\sqrt{\frac{\sum d^{2}}{n}-\left(\frac{\sum d}{n}\right)^{2}}=\sqrt{\frac{112}{6}-\left(\frac{0}{6}\right)^{2}}=4.31 \\
& \therefore \mathrm{C} . \mathrm{V}=\frac{\sigma}{x} \times 100=\frac{4.31}{30} \times 10=14.36
\end{aligned}
$$

The time taken (in minutes) to complete a homework by 8 students in a day are given by $38,40,47$, $44,46,43,49,53$. Find the coefficient of variation.
Solution : Given data is $38,40,47,44,46,43,49,53$.

$$
\bar{x}=\frac{38+40+47+44+46+43+49+53}{8}=\frac{360}{8}=45
$$



$$
\begin{aligned}
& \therefore \sigma=\sqrt{\frac{\sum d^{2}}{n}-\left(\frac{\sum d}{n}\right)^{2}}=\sqrt{\frac{164}{8}-\left(\frac{0}{8}\right)^{2}}=4.53 \\
& \therefore C . V=\frac{\sigma}{x} \times 100=\frac{4.53}{45} \times 100=10.07
\end{aligned}
$$

The marks scored by 10 students in a class test are $25,29,30,33,35,37,38,40,44,48$. Find the standard deviation.

| Solution : | $\boldsymbol{x}$ | $\mathrm{d}=\boldsymbol{x}-35$ | $\mathrm{~d}^{2}$ |
| :---: | :---: | :---: | :---: |
|  | 25 | -10 | 100 |
| 29 | 6 | 36 |  |
| 30 | -5 | 25 |  |
|  | 33 | -2 | 4 |
|  | 35 | 0 | 0 |
|  | 37 | 2 | 4 |
|  | 38 | 3 | 9 |
| 40 | 5 | 25 |  |
|  | 44 | 9 | 81 |
| 48 | 13 | 169 |  |
|  | $\mathbf{n}=10$ | 9 | 453 |

## A ZAYAAN ABDUL M.SC.BED JAYANIGONDAM,ARIYALUR DI

$$
\begin{aligned}
\therefore \sigma & =\sqrt{\frac{\sum d^{2}}{n}-\left(\frac{\sum d}{n}\right)^{2}} \\
& =\sqrt{\frac{453}{10}-\left(\frac{9}{10}\right)^{2}} \\
& =6.67
\end{aligned}
$$

## 8 MARKS

## GRAPH

1. Determine the nature of roots for the following quadratic equation $2 x^{2}-2 x+9=0$
2. Determine the nature of roots for the following quadratic equation $x^{2}-x-20=0$
3. Determine the nature of roots for the following quadratic equation $9 x^{2}-24 x+16=0$
4. Determine the nature of roots for the following quadratic equation $x^{2}-9 x+20=0$
5. Determine the nature of roots for the following quadratic equation $x^{2}-4 x+4=0$
6. Determine the nature of roots for the following quadratic equation $x^{2}+x+7=0$
7. Determine the nature of roots for the following quadratic equation $x^{2}-9=0$
8. Determine the nature of roots for the following quadratic equation $x^{2}-6 x+9=0$
9. Determine the nature of roots for the following quadratic equation $(2 x-3)(x+2)=0$

## 8MARKS <br> GEOMETRY

1. Construct a triangle similar to a given triangle $P Q R$ with its sides equal to $\frac{2}{3}$ of the corresponding sides of the triangle $P Q R$ (scale factor $\frac{2}{3}$ ).
2. Construct a triangle similar to a given triangle $L M N$ with its sides equal to $\frac{4}{5}$ of the corresponding sides of the triangle $L M N$ (scale factor $\frac{4}{5}$ ).
3. Construct a triangle similar to a given triangle $A B C$ with its sides equal to $\frac{6}{5}$ of the corresponding sides of the triangle $A B C$ (scale factor $\frac{6}{5}$ ).
4. Construct a triangle similar to a given triangle $P Q R$ with its sides equal to $\frac{7}{3}$ of the corresponding sides of the triangle $P Q R$ (scale factor $\frac{7}{3}$ ).
5. Draw a circle of radius 4 cm . At a point $L$ on it draw a tangent to the circle using the alternate segment.
6. Draw a circle of diameter 6 cm from a point $P$, which is 8 cm away from its centre. Draw the two tangents $P A$ and $P B$ to the circle and measure their lengths.
7. Draw a circle of radius 4.5 cm . Take a point on the circle. Draw the tangent at that point using the alternate segment theorem.
8. Draw the two tangents from a point which is 10 cm away from the centre of a circle of radius 5 cm . Also, measure the lengths of the tangents.
9. Take a point which is 11 cm away from the centre of a circle of radius 4 cm and draw the two tangents to the circle from that point.
10.Draw the two tangents from a point which is 5 cm away from the centre of a circle of diameter 6 cm . Also, measure the lengths of the tangents.
10. Draw a tangent to the circle from the point $P$ having radius 3.6 cm , and centre at $O$. Point $P$ is at a distance 7.2 cm from the centre.

## I. RELATIONS AND FUNCTION

Let $A=\{1,2,3,4\}$ and $B=N$. Let $f: A \rightarrow B$ be defined by $f(x)=x^{3}$ then, (i) find the range of $f$ (ii) identify the type of function

Solution : $\mathrm{A}=\{1,2,3,4\}, \mathrm{B}=\mathrm{N} \quad f(x)=x^{3}$

$$
x=1 \Rightarrow f(1)=1 \quad x=3 \Rightarrow f(3)=27
$$

$$
x=2 \Rightarrow f(2)=8 \quad x=4 \Rightarrow f(4)=64
$$

(i) Range of $f=\{1,8,27,64\} \quad$ (ii) $f$ is one-one

## A function $f$ is defined by $f(x)=3-2 x$. Find $x$ such that $f\left(x^{2}\right)=(f(x))^{2}$.

Solution :

$$
\begin{array}{ll}
: f(x)=3-2 x \text { and } & f\left(x^{2}\right)=(f(x))^{2} \\
\Rightarrow 3-2 x^{2}=(3-2 x)^{2} & \Rightarrow(x-1)^{2}=0 \\
\Rightarrow x=1 \text { (twice) }
\end{array}
$$

The Cartesian product $A \times A$ has 9 elements among which $(-1,0)$ and $(0,1)$ are found. Find the set $A$ and the remaining elements of $A \times A$.
Solution : $n(A \times A)=9$ and $(-1,0),(0,1) \in A \times A$
$\therefore A=\{-1,0,1\}$
The remaining elements of $\mathbf{A} \times \mathbf{A}=\{(-1,-1),(-1,1),(0,-1),(0,0),(1,-1),(1,0),(1,1)\}$
Find the domain of the function $\boldsymbol{f}(\boldsymbol{x})=\sqrt{1+\sqrt{1-\sqrt{1-\boldsymbol{x}^{2}}}}$.
Solution: If $x>1$ and $x<-1, f(x)$ leads to unreal
$\therefore$ The domain of $f(x)=\{-1,0,1\}$
If the ordered palrs $\left(x^{2}-3 x, y^{2}+4 y\right)$ and $(-2,5)$ are equal, then find $x$ and $y$.
Solution: Given $\left(x^{2}-3 \mathrm{x}, y^{2}+4 y\right)=(-2,5)$

$$
\begin{array}{l|l}
x^{2}-3 x=-2 & y^{2}+4 y=5 \\
x=2,1 & y=-5,1
\end{array}
$$

Let $X=\{3,4,6,8\}$. Determine whether the relation $R=\left\{(x, f(x)) \mid x \in X, f(x)=x^{2}+1\right\}$ is a function
from $X$ to $N$ ?
Sohution : $\mathrm{X}=\{3,4,6,8\} \quad \mathrm{R}=\left\{(\mathrm{x}, \mathrm{f}(\mathrm{x})) \mid \mathrm{x} \in \mathrm{X}, \mathrm{f}(\mathrm{x})=\mathrm{x}^{\mathbf{2}}+1\right\}$ $x=3 \Rightarrow \mathrm{f}(3)=9+1=10 \quad x=6 \Rightarrow \mathrm{f}(6)=36+1=37$ $x=4 \Rightarrow \mathrm{f}(4)=16+1=17 \quad x=8 \Rightarrow \mathrm{f}(8)=64+1=65$
$R=\{(3,10),(4,17),(6,37),(8,65)\} \quad \therefore$ The relation $R: X \rightarrow N$ is a function

```
Solution :
\[
f(x)=x^{2}-2
\]
(ii) If \(f\) a function?
\[
x \in\{-2,-1,0,3\}
\]
```

(i) $x \in\{-2,-1,0,3\}$
$f(-2)=(-2)^{2}-2=2 ; f(-1)=(-1)^{2}-2=-1$
$f(0)=(0)^{2}-2=-2 ; f(3)=(3)^{2}-2=7$
$\mathrm{f}(0)=(0)^{2}-2=-2 ; f(3)=(3)^{2}-2=7$
$f=\{(-2,2),(-1,-1),(0,-2),(3,7)\}$
(ii) Since all the elements has unique image. $f$ is a function.

## Let $f(x)=2 x+5$. If $x \neq 0$ then find $\quad f(x+2)-f(2)$

## Solution :

$\mathrm{f}(\mathrm{x})=2 \mathrm{x}+5$
$\mathrm{f}(\mathrm{x}+2)=2(x+2)+5=2 x+9$
$\mathrm{f}(2)=2(2)+5=9$
$\therefore \frac{f(x+2)-f(x)}{x}=\frac{2 x+9-9}{x}=2$

Let $A=\{9,10,11,12,13,14,15,16,17\}$ and let $f: A \rightarrow N$ be defined by $f(n)=$ the highest prime factor of $n \in A$. Write $f$ as a set of ordered pairs and find the range of $f$
Solution :
$f=\{(9,3),(10,5),(11,11),(12,3),(13,13),(14,7),(15,5),(16,2),(17,17)\}$
Range of $f=\{2,3,5,7,11,13,17\}$

Let $A=\{1,2\}$ and $B=\{1,2,3,4\}, C=\{5,6\}$ and $D=\{5,6,7,8\}$. Verify whether $A \times C$ is a subset of $\mathbf{B} \times \mathbf{D}=$ ?
Solution : $A=\{1,2\}, B=\{1,2,3,4\}, C=\{5,6\}, D=\{5,6,7,8\}$

$$
A \times C=\{(1,5),(1,6),(2,5),(2,6)\}
$$

$B \times D=\{(1,5),(1,6),(1,7),(1,8),(2,5),(2,6),(2,7),(2,8),(3,5),(3,6),(3,7),(3,8),(4,5),(4,6)$, $(4,7),(4,8)$.

$$
\therefore \mathbf{A} \times \mathbf{C} \text { is a subset of } \mathbf{B} \times \mathbf{D} .
$$

## If $f: \mathbf{R} \rightarrow \mathbf{R}$ and $g: R \rightarrow R$ are defined by $f(x)=x^{5}$ and $g(x)=x^{4}$ then check if $f, g$ are one-one and $f \circ g$ is one-one?

Solution : Let $\mathbf{A}$ be the domain. B be the co-domain.
For every element $A$, there is a umique image in $B$.
Since $f$ is an odd function
$\therefore f$ is $1-1$.
$g(x)$ is an even function.
$\therefore$ Two elements of domain will have image in co-domain. $\therefore g$ is not $1-1$.

## Let $f(x)=x^{2}-1$. Find fof <br> Solution : $\quad(f \circ f)=\left(x^{2}-1\right)\left(x^{2}-1\right)=\left(x^{2}-1\right)^{2}-1=x^{4}-2 x^{2}+1-1=x^{4}-2 x^{2}$

Let $A=\{3,4,7,8\}$ and $B=\{1,7,10\} . R_{3}=\{(3,7),(4,10),(7,7),(7,8),(8,11),(8,7),(8,10)\}$ are relations from $A$ to $B$ ?
Solution : $\mathbf{A} \times \mathbf{B}=\{(3,1),(3,7),(3,10),(4,1),(4,7),(4,10),(7,1),(7,7),(7,10),(8,1),(8,7),(8,10)\}$
$\mathbf{R}_{3}=\{(3,7),(4,10),(7,7),(7,8),(8,11),(8,7),(8,10)\}$
$(7,8) \in R_{3}$, but $(7,8) \notin A \times B$. So $R_{3}$ is not a relation from $A$ to $B$.

$$
\begin{aligned}
& \text { If } f(x)=x^{2}-1, \text { find } f \circ f \circ f \\
& \text { Solution : } \begin{aligned}
(f \circ f)=\left(\left(x^{2}-1\right)^{2}-1\right) \\
(f \circ f \circ f)(x)=\left(x^{4}-2 x^{2}\right)^{2}-1
\end{aligned}
\end{aligned}
$$

$\boldsymbol{f}: \mathbf{R} \rightarrow \mathbf{R}$ defined by $\boldsymbol{f}(\boldsymbol{x})=\mathbf{2 x + 1}$ whether the function is bijective or not. Justify your answer.
Solution : $f: \mathbf{R} \rightarrow \mathrm{R}$ defined by $f(x)=2 x+1$
Let $f\left(x_{1}\right)=f\left(x_{2}\right)$
$\Rightarrow 2 x_{1}+1=2 x_{2}+1 \Rightarrow 2 x_{1}=2 x_{2} \Rightarrow x_{1}=x_{2} \quad \therefore f\left(x_{1}\right)=f\left(x_{2}\right) \Rightarrow x_{1}=x_{2}$ $\therefore f$ is $1-1$ function.
$y=2 x+1 \Rightarrow \therefore 2 x=y-1 \Rightarrow x=\frac{y-1}{2} \quad \therefore f(x)=2\left(\frac{y-1}{2}\right)+1=y \quad \therefore f$ is onto. $\therefore f$ is one-one and onto $\Rightarrow f$ is bijective.

Find $k$ if $f \circ f(k)=5$ where $f(k)=2 k-1$.
Solution: $\quad f \circ f(k)=(2 k-1)(2 k-1)=2(2 k-1)-1=4 k-3$.

$$
f \circ f(k)=5 \Rightarrow 4 k-3=5 \Rightarrow 4 k=5+3 \Rightarrow 4 k=8 \Rightarrow k=2
$$

Represent the function $f(x)=\sqrt{2 x^{2}-5 x+3}$ as a composition of two functions.
Solution : $f_{2}(x)=2 x^{2}-5 x+3$ and $f_{1}(x)=\sqrt{x}$

$$
f(x)=\sqrt{2 x^{2}-5 x+3}=\sqrt{f_{2}(x)}=f_{1} f_{2}(x)
$$

$$
\begin{aligned}
& \text { If } A \times B=\{(3,2),(3,4),(5,2),(5,4)\} \text { then find } A \text { and } B . \\
& \text { Solution: } A \times B=\{(3,2),(3,4),(5,2),(5,4)\} \\
& \qquad A=\{3,5\} \text { and } B=\{2,4\} .
\end{aligned}
$$

## If $\mathbf{A}=\mathbf{B}=\{p, q\}$ find $\mathbf{A} \times \mathbf{B}, \mathbf{A} \times \mathbf{A}$ and $\mathbf{B} \times \mathbf{A}$

Solution: $\mathrm{A} \times \mathrm{B}=\mathrm{A} \times \mathrm{A}=\mathrm{B} \times \mathrm{A}=\{p, q\} \times\{p, q\}=\{(p, p),(p, q),(q, p),(q, q)\}$

## If $\mathbf{A}=\{m, n\}$ and $B=\phi$ then find $\mathbf{A} \times \mathbf{B}, \mathbf{A} \times \mathbf{A}$ and $\mathbf{B} \times \mathbf{A}$

## Solution:

$A \times B=B \times A=\phi$ and
$\mathrm{A} \times \mathrm{A}=\{(m, m),(m, n),(n, m),(n, n)\}$
Let $A=\{1,2,3\}$ and $B=\{x \mid x$ is a prime number less than 10$\}$. Find $A \times B$ and $B \times A$.
Solution: $\mathbf{A}=\{1,2,3\}, B=\{x \mid x$ is a prime number less than 10$\}=\{2,3,5,7\}$ $A \times B=\{(1,2),(1,3),(1,5),(1,7),(2,2),(2,3),(2,5),(2,7),(3,2),(3,3),(3,5),(3,7)\}$ $B \times \mathbf{A}=\{(2,1),(2,2),(2,3),(3,1),(3,2),(3,3),(5,1),(5,2),(5,3),(7,1),(7,2),(7,3)\}$
If $B \times A=\{(-2,3),(-2,4),(0,3),(0,4),(3,3),(3,4)\}$ find $A$ and $B$.
Solution : $B \times A=\{(-2,3),(-2,4),(0,3),(0,4),(3,3),(3,4)\}$

$$
\therefore B=\{-2,0,3\}, A=\{3,4\}
$$

If $A \times B=\{(3,2),(3,4),(5,2),(5,4)\}$ then find $A$ and $B$.
Solution: $A \times B=\{(3,2),(3,4),(5,2),(5,4)\}$
$A=\{3,5\}$ and $B=\{2,4\}$.
If $A=\{2,-2,3\}$ and $B=\{1,-4\}$ then find $A \times B$ and $B \times A$
Solution: Given $A=\{2,-2,3\}, B=\{1,-4\}$
$A \times B=\{2,-2,3\} \times\{1,-4\}=\{(2,1),(2,-4),(-2,1),(-2,-4),(3,1),(3,-4)\}$
$B \times A=\{1,-4\} \times\{2,-2,3\}=\{(1,2),(1,-2),(1,3),(-4,2),(-4,-2),(-4,3)\}$
If $\mathbf{A}=\mathbf{B}=\{p, q\}$ find $\mathbf{A} \times \mathbf{B}, \mathbf{A} \times \mathbf{A}$ and $\mathbf{B} \times \mathbf{A}$
Solution: $\mathbf{A} \times \mathbf{B}=\mathbf{A} \times \mathbf{A}=\mathbf{B} \times \mathbf{A}=\{p, q\} \times\{p, q\}=\{(p, p),(p, q),(q, p),(q, q)\}$

## If $\mathbf{A}=\{\boldsymbol{m}, \boldsymbol{n}\}$ and $\mathbf{B}=\phi$ then find $\mathbf{A} \times \mathbf{B}, \mathbf{A} \times \mathbf{A}$ and $\mathbf{B} \times \mathbf{A}$

Solution: $\mathrm{A} \times \mathrm{B}=\mathrm{B} \times \mathrm{A}=\phi$ and $\mathrm{A} \times \mathrm{A}=\{(m, m),(m, n),(n, m),(n, n)\}$
Let $A=\{1,2,3\}$ and $B=\{x \mid x$ is a prime number less than 10$\}$. Find $A \times B$ and $B \times A$.
Solution : $\mathbf{A}=\{1,2,3\}, \mathrm{B}=\{x \mid x$ is a prime number less than 10$\}=\{2,3,5,7\}$
$A \times B=\{(1,2),(1,3),(1,5),(1,7),(2,2),(2,3),(2,5),(2,7),(3,2),(3,3),(3,5),(3,7)\}$
$B \times A=\{(2,1),(2,2),(2,3),(3,1),(3,2),(3,3),(5,1),(5,2),(5,3),(7,1),(7,2),(7,3)\}$
If $B \times A=\{(-2,3),(-2,4),(0,3),(0,4),(3,3),(3,4)\}$ find $A$ and $B$.
Solution: $\mathbf{B} \times \mathbf{A}=\{(-2,3),(-2,4),(0,3),(0,4),(3,3),(3,4)\}$
$B=\{-2,0,3\}, A=\{3,4\}$

Define - Cartesian Product
If $\mathbf{A}$ and B are two non-empty sets, then the set of all ordered pairs ( $a, b$ ) such that $a \in A, b \in B$ is called the Cartesian Product of $\mathbf{A}$ and B , and is denoted by $\mathbf{A} \times \mathbf{B}$. Thus, $\mathbf{A} \times \mathbf{B}=\{(a, b) \mid a \in \mathbf{A}, b \in \mathrm{~B}\}$
Define - Relation
A relation $f$ between two non-empty sets $X$ and $Y$ is called a function from $X$ to $Y$ if, for each $x \in X$ there exists only one $y \in \mathrm{Y}$ such that $(x, y) \in f$. That is, $f=\{(x, y) \mid$ for all $x \in X, y \in \mathrm{Y}\}$.
The arrow diagram shows a relationship between the sets $P$ and $Q$. Write the relation in (i) Set builder form (ii) Roster form (iii) What is the domain and range of $R$.
Solution : (i) Set builder form $R=\{(x, y) \mid y=x-2, x \in P, y \in Q\}$
(ii) Roster form $R=\{(5,3),(6,4),(7,5)\}$
(iii) Domain $=\{5,6,7\}$ and Range $=\{3,4,5\}$


Let $A=\{1,2,3,4 \ldots, 45\}$ and $R$ be the relation defined as "is square of" on $A$. Write $R$ as a subset of $A \times A$. Also, find the domain and range of $R$.
Solution : $A=\{1,2,3,4, \ldots \ldots . .45\}$ and $R$ 'is square of" on $A . \Rightarrow R=\{1,4,9,16,25,36\}$ $R$ is a subset of $A$.
$\therefore$ Domain $=\{1,2,3,4,5,6\} \quad \therefore$ Range $=\{1,4,9,16,25,36\}$
Let $A=\{1,2,3,7\}$ and $B=\{3,0,-1.7), R_{4}=\{(7,-1),(0,3),(3,3),(0,7)\}$ are relation from $A$ to $B$ ? Solution : $\therefore \mathbf{A} \times \mathbf{B}=\{(1,3),(1,0),(1,-1),(1,7),(2,3),(2,0),(2,-1),(2,7),(3,3),(3,0),(3,-1),(3,7)$,

$$
(7,3),(7,0),(7,-1),(7,7)\}
$$

$\mathbf{R}_{4}=\{(7,-1),(0,3),(3,3),(0,7)\}$ and $(0,3),(0,7) \in R_{4}$ but not in $\mathbf{A} \times \mathbf{B}$. $\therefore \mathbf{R}_{4}$ is not a relation.

## 2.NUMBERS AND SEDUENCES

Find the $12^{\text {th }}$ term from the last term of the $A . P-2,-4,-6, \ldots-100$.
Solution : Given A.P is $-2,-4,-6, \ldots .-100 \quad a=-100, \mathrm{~d}=2$

$$
\mathrm{t}_{12}=a+11 \mathrm{~d}=-100+11(2)=-100+22=-78
$$

## Find the $8^{\mathrm{m}}$ term of the G.P. 9.3.1, ...

Solution: First term $a=9$, common ratio $r=\frac{t_{2}}{t_{1}}=\frac{3}{9}=\frac{1}{3}$

$$
t_{8}=9 \times\left(\frac{1}{3}\right)^{8-1}=9 \times\left(\frac{1}{3}\right)^{7}=\frac{1}{243}
$$

## Write the Fundamental theorem of arithmetic

Every natural number except 1 can be factorized as a product of primes and this factorization is unique except for the order in which the prime factors are written

$$
\begin{aligned}
& \text { In a G.P. 729, 243, 81, } \ldots \text { find } t_{r} . \\
& \text { Solution: } 729,243,21, \ldots \ldots . . \quad \begin{array}{l}
a=729 \quad r=8 / 243=1 / 3 \\
\quad \therefore t_{n}=a \cdot r^{n-1}
\end{array} \\
& \Rightarrow t_{7}=a \cdot r^{6}=729 \times(1 / 3)^{6}=729 \times(1 / 729)=1
\end{aligned}
$$

## Find the sum of all odd positive integers less than 450 .

Solution : $1+3+5+7+\ldots \ldots . . .+449=\left[\frac{(l+1)}{2}\right]^{2}=\left[\frac{449+1}{2}\right]^{2}=\left[\frac{450}{2}\right]^{2}=[225]^{2}=50,625$

## 3. ALGEBRA

Define - Matrix.
A matrix is a rectangular array of elements. The horizontal arrangements are called rows and vertical
arrangements are called columns. Example: $A=\left(\begin{array}{cc}23 & 18 \\ 47 & 36 \\ 15 & 16\end{array}\right)$

| Write the three conditions of nature of roots. |  |  |
| :--- | :--- | :--- |
| Solution : |  |  |
| Values of Discriminant $\Delta=b^{2}-4 a c$ | Real and Unequal roots | $\Delta>0$ |
|  | Real and Equal roots | $\Delta=0$ |
|  | No Real root | $\Delta<0$ |

If $\left(\begin{array}{ccc}5 & 4 & 3 \\ 1 & -7 & 9 \\ 3 & 8 & 2\end{array}\right)$ then find the transpose of $A$. Solution : $A=\left(\begin{array}{ccc}5 & 4 & 3 \\ 1 & -7 & 9 \\ 3 & 8 & 2\end{array}\right) \therefore A^{T}=\left(\begin{array}{ccc}5 & 1 & 3 \\ 4 & -7 & 8 \\ 3 & 9 & 2\end{array}\right)$

If a matrix has 18 elements, what are the possible orders it can have? What if it has 6 elements? Solution: Given, a matrix has 18 elements. The possible orders $18 \times 1,1 \times 18,9 \times 2,2 \times 9,6 \times 3,3 \times 6$ The matrix has 6 elements. The order are $1 \times 6,6 \times 1,3 \times 2,2 \times 3$
If $A=\left(\begin{array}{lr}\sqrt{7} & -3 \\ -\sqrt{5} & 2 \\ \sqrt{3} & -5\end{array}\right)$ then find the transpose of-A.
Solution : $-A=\left(\begin{array}{ll}-\sqrt{7} & 3 \\ \sqrt{5} & -2 \\ -\sqrt{3} & 5\end{array}\right) \quad \therefore$ Transpose of $-A=\left(\begin{array}{ccc}-\sqrt{7} & \sqrt{5} & -\sqrt{3} \\ 3 & -2 & 5\end{array}\right)$
Define - diagonal matrix.
A square matrix, all of whose elements, except those in the leading diagonal are zero is called a diagonal matrix. Example:

$$
A=\left(\begin{array}{ccc}
5 & 0 & 0 \\
0 & -7 & 0 \\
0 & 0 & 2
\end{array}\right)
$$

Define-scalar matrix
A diagonal matrix in which all the leading diagonal elements are equal is called a scalar matrix.
Example:

$$
A=\left(\begin{array}{lll}
3 & 0 & 0 \\
0 & 3 & 0 \\
0 & 0 & 3
\end{array}\right)
$$

Simplify $\frac{x^{3}}{x-y}+\frac{y^{3}}{y-x}$
Solution : $\frac{x^{3}}{x-y}+\frac{y^{3}}{y-x}=\frac{x^{3}}{x-y}-\frac{y^{3}}{x-y}$

$$
=\frac{x^{3}-y^{3}}{x-y}=\frac{(x-y)\left(x^{2}+x y+y^{2}\right)}{x-y}=x^{2}+x y+y^{2}
$$

Subtract $\frac{1}{x^{2}+2}$ from $\frac{2 x^{3}+x^{2}+3}{\left(x^{2}+2\right)^{2}}$
Solution:

$$
\frac{2 x^{3}+x^{2}+3}{\left(x^{2}+2\right)^{2}}-\frac{1}{x^{2}+2}=\frac{\left(2 x^{3}+x^{2}+3\right)-\left(x^{2}+2\right)}{\left(x^{2}+2\right)^{2}}=\frac{2 x^{3}+x^{2}+3-x^{2}-2}{\left(x^{2}+2\right)^{2}}=\frac{2 x^{3}+1}{\left(x^{2}+2\right)^{2}}
$$

Find the square root of $16 x^{2}+9 y^{2}-24 x y+24 x-18 y+9$
Solution : $\sqrt{16 x^{2}+9 y^{2}-24 x y+24 x-18 y+9}=\sqrt{(4 x-3 y+3)^{2}}=|4 x-3 y+3|$
Solve $x^{4}-13 x^{2}+42=0$
Solution: $\quad\left(x^{2}\right)^{2}-13 x^{2}+42=0$

$$
\begin{aligned}
\left(x^{2}\right)^{2}-13 x^{2}+42 & =0 \\
\left(x^{2}-7\right)\left(x^{2}-6\right) & =0 \quad \Rightarrow x= \pm \sqrt{7} \text { or } \quad x= \pm \sqrt{6} .
\end{aligned}
$$

If the difference between a number and its reciprocal is $\frac{24}{5}$, find the number.
Solution : Let $x$ be the required number $\frac{1}{x}$ be its reciprocal $\quad$ Given $x-\frac{1}{x}=\frac{24}{5}$

$$
\Rightarrow \frac{x^{2}-1}{x}=\frac{24}{5} \Rightarrow 5 x^{2}-24 x-5=0 \Rightarrow \therefore \text { The required numbers are } 5,-1 / 5
$$

Find the excluded values of $\frac{x}{x^{2}+1}$ expressions
Solution: $\mathrm{x}^{2}+1 \neq 0$ for any $x$. Therefore, no real excluded values
Reduce to lowest form. $\frac{x^{2}-1}{x^{2}+x}$ Solution : $\frac{x^{2}-1}{x^{2}+x}=\frac{(x+1)(x-1)}{x(x+1)}=\frac{x-1}{x}$
Simplify $\frac{x^{3}-y^{3}}{3 x^{2}+9 x y+6 y^{2}} \times \frac{x^{2}+2 x y+y^{2}}{x^{2}-y^{2}}$
Solution : $\frac{x^{3}-y^{3}}{3 x^{2}+9 x y+6 y^{2}} \times \frac{x^{2}+2 x y+y^{2}}{x^{2}-y^{2}}=\frac{(x-y)\left(x^{2}+x y+y^{2}\right)}{3\left(x^{2}+3 x y+2 y^{2}\right)} \times \frac{(x+y)(x+y)}{(x+y)(x-y)}$

$$
\begin{aligned}
& =\frac{\left(x^{2}+x y+y^{2}\right)(x+y)}{3(x+2 y)(x+y)} \\
& =\frac{x^{2}+x y+y^{2}}{3(x+2 y)}
\end{aligned}
$$

Simplify $\frac{x^{2}-16}{x+4} \div \frac{x-4}{x+4}$
Solution : $\frac{x^{2}-16}{x+4}+\frac{x-4}{x+4}=\frac{(x+4)(x-4)}{(x+4)} \times\left(\frac{x+4}{x-4}\right)=x+4$
Reduce to lowest form $\frac{x^{3 a}-8}{x^{2} a+2 x a+4}$
Solution : $\frac{x^{3 a}-8}{x^{2} a+2 x a+4}=\frac{\left(x^{a}-2\right)\left(x^{2 a}+2 x^{e}+4\right)}{x^{2 a}+2 x^{a}+4}=x^{a}-2$


If $A=\left(\begin{array}{cc}\cos \theta & 0 \\ 0 & \cos \theta\end{array}\right), B=\left(\begin{array}{cc}\sin \theta & 0 \\ 0 & \sin \theta\end{array}\right)$ then show that $A^{2}+B^{2}=\mathbf{I}$.
Solution : $A=\left(\begin{array}{cc}\cos \theta & 0 \\ 0 & \cos \theta\end{array}\right), B=\left(\begin{array}{cc}\sin \theta & 0 \\ 0 & \sin \theta\end{array}\right)$
$A^{2}=\left(\begin{array}{cc}\cos \theta & 0 \\ 0 & \cos \theta\end{array}\right)\left(\begin{array}{cc}\cos \theta & 0 \\ 0 & \cos \theta\end{array}\right)=\left(\begin{array}{cc}\cos ^{2} \theta & 0 \\ 0 & \cos ^{2} \theta\end{array}\right)$
$\mathbf{B}^{2}=\left(\begin{array}{cc}\sin \theta & 0 \\ 0 & \sin \theta\end{array}\right)\left(\begin{array}{cc}\sin \theta & 0 \\ 0 & \sin \theta\end{array}\right)=\left(\begin{array}{cc}\sin ^{2} \theta & 0 \\ 0 & \sin ^{2} \theta\end{array}\right)$
$\therefore A^{2}+B^{2}=\left(\begin{array}{cc}\cos ^{2} \theta+\sin ^{2} \theta & 0 \\ 0 & \cos ^{2} \theta+\sin ^{2} \theta\end{array}\right)=\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)=\mathbf{I}$.
If $A=\left(\begin{array}{ccc}1 & 3 & -2 \\ 5 & -4 & 6\end{array}\right) B=\left(\begin{array}{ll}1 & 8 \\ 3 & 4\end{array}\right)$ find $A+B$. Solution : $A$ is of order $3 \times 3 B$ is of order $3 \times 2$
$\left(\begin{array}{ccc} & 2 & 9 \\ -3 & 2 & \text { It is not possible to add } A \text { and } B \text { because different orders. } \\ 9 & 6\end{array}\right) \quad$.
Given $A=\left(\begin{array}{ll}p & 0 \\ 0 & 2\end{array}\right), B=\left(\begin{array}{cc}0 & -q \\ 1 & 0\end{array}\right), C=\left(\begin{array}{cc}2 & -2 \\ 2 & 2\end{array}\right)$ and if $B A=C^{2}$, find $p$ and $q$.
Solution : Given $B A=C^{2} \Rightarrow\left(\begin{array}{cc}0 & -q \\ 1 & 0\end{array}\right)\left(\begin{array}{cc}p & 0 \\ 0 & 2\end{array}\right)=\left(\begin{array}{cc}2 & -2 \\ 2 & 2\end{array}\right)\left(\begin{array}{cc}2 & -2 \\ 2 & 2\end{array}\right) \Rightarrow\left(\begin{array}{cc}0 & -2 q \\ p & 0\end{array}\right)=\left(\begin{array}{cc}0 & -8 \\ 8 & 0\end{array}\right)$

$$
\begin{aligned}
\therefore p=8,-2 q & =-8, \\
q & =4
\end{aligned}
$$

If $A=\left(\begin{array}{cc}\cos \theta & \sin \theta \\ -\sin \theta & \cos \theta\end{array}\right)$ prove that $A A^{\mathrm{T}}=\mathbf{I}$
Solution : $A A^{T}=\left(\begin{array}{cc}\cos \theta & \sin \theta \\ -\sin \theta & \cos \theta\end{array}\right)\left(\begin{array}{cc}\cos \theta & -\sin \theta \\ \sin \theta & \cos \theta\end{array}\right)=\left(\begin{array}{cc}\cos ^{2} \theta+\sin ^{2} \theta & -\cos \theta \sin \theta+\sin \theta \cos \theta \\ -\sin \theta \cos \theta+\cos \theta \sin \theta & \sin ^{2} \theta+\cos ^{2} \theta\end{array}\right)=\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)=I$ Hence proved.

$$
\begin{aligned}
& \text { If } A=\left(\begin{array}{ccc}
5 & 2 & 2 \\
-\sqrt{17} & 0.7 & \frac{5}{2} \\
8 & 3 & 1
\end{array}\right) \begin{array}{r}
\text { then verify }\left(A^{T}\right)^{T}=\mathbf{A} \\
\text { Solution: } \\
A^{T}
\end{array}=\left(\begin{array}{ccc}
5 & -\sqrt{17} & 8 \\
2 & 0.7 & 3 \\
2 & 5 / 2 & 1
\end{array}\right) \\
&\left(A^{T}\right)^{T}=\left(\begin{array}{ccc}
5 & 2 & 2 \\
-\sqrt{17} & 0.7 & 5 / 2 \\
8 & 3 & 1
\end{array}\right)=A
\end{aligned}
$$

Construct a $3 \times 3$ matrix whose elements are given by $a_{i j}=|i-2 j|$
Solution:

$$
\text { Given } a_{i j}=|\mathrm{i}-2 \mathrm{j}|, 3 \times 3 \quad A=\left(\begin{array}{lll}
a_{11} & a_{12} & a_{13} \\
a_{21} & a_{22} & a_{23} \\
a_{31} & a_{32} & a_{33}
\end{array}\right) \quad \therefore A=\left(\begin{array}{lll}
1 & 3 & 5 \\
0 & 2 & 4 \\
1 & 1 & 3
\end{array}\right)
$$

Find the square root $\frac{7 x^{2}+2 \sqrt{14} x+2}{x^{2}-\frac{1}{2} x+\frac{1}{16}}$
Solution : $\sqrt{\frac{7 x^{2}+2 \sqrt{14} x+2}{x^{2}-\frac{1}{2} x+\frac{1}{16}}}=\sqrt{\frac{(\sqrt{7} x+\sqrt{2})^{2}}{\left(x-\frac{1}{4}\right)^{2}}}=4\left|\frac{\sqrt{7} x+\sqrt{2}}{(4 x-1)}\right|$
Find the square root of $4 x^{2}+20 x+25$
Solution:

$$
\sqrt{4 x^{2}+20 x+25}=\sqrt{(2 x+5)^{2}}=|2 x+5|
$$

Find the square root of $9 \mathrm{x}^{2}-24 \mathrm{xy}+30 \mathrm{xz}-40 \mathrm{yz}+25 \mathrm{z}^{2}+16 \mathrm{y}^{2}$
Solution : $\sqrt{9 x^{2}-24 x y+30 x-40 y z+25 z^{2}+16 y^{2}}=\sqrt{(3 x-4 y+5 z)^{2}}=|3 x-4 y+5 z|$

## Find the square root of $1+\frac{1}{x^{6}}+\frac{2}{x^{3}}$

Solution : $\sqrt{1+1 / x^{6}+2 / x^{3}}=\sqrt{\left(1+1 / x^{3}\right)^{2}}=\left|1+1 / x^{3}\right|$
Find the square root of $16 x^{1}+8 x^{\mathbf{2}}+1$ by division method
Solution : $\sqrt{16 x^{4}+8 x^{2}+1}=\sqrt{\left(4 x^{2}+1\right)^{2}}=\left|4 x^{2}+1\right|$
Verify that $A^{2}=I$ when $A=\left(\begin{array}{ll}5 & -4 \\ 6 & -5\end{array}\right)$
Solution : $A=\left(\begin{array}{ll}5 & -4 \\ 6 & -5\end{array}\right) \quad A^{2}=A A=\left(\begin{array}{ll}5 & -4 \\ 6 & -5\end{array}\right)\left(\begin{array}{ll}5 & -4 \\ 6 & -5\end{array}\right)=\left(\begin{array}{ll}25-24 & -20+20 \\ 30-30 & -24+25\end{array}\right)=\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)=\mathrm{I}$
If $\cos \theta\left(\begin{array}{cc}\cos \theta & \sin \theta \\ -\sin \theta & \cos \theta\end{array}\right)+\sin \theta\left(\begin{array}{cc}x & -\cos \theta \\ \cos \theta & x\end{array}\right)=I_{2}$ find $x$
Solution: $\quad \cos \theta\left(\begin{array}{cc}\cos \theta & \sin \theta \\ -\sin \theta & \cos \theta\end{array}\right)+\sin \theta\left(\begin{array}{cc}x & -\cos \theta \\ \cos \theta & x\end{array}\right)=I_{2} \Rightarrow\left(\begin{array}{cc}\cos ^{2} \theta+x \sin \theta & 0 \\ 0 & \cos ^{2} \theta+x \sin \theta\end{array}\right)=\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)$

$$
\Rightarrow \cos ^{2} \theta+x \sin \theta=1 \Rightarrow x=\sin \theta
$$

Show that the matrices $A=\left(\begin{array}{ll}1 & 2 \\ 3 & 1\end{array}\right), B=\left(\begin{array}{cc}1 & -2 \\ -3 & 1\end{array}\right)$ satisfy commutative propertyAB=BA
Solution :

$$
\therefore \mathbf{A B}=\mathbf{B A}
$$

$\therefore$ commutative property is true.

$$
\begin{aligned}
& A B=\left(\begin{array}{ll}
1 & 2 \\
3 & 1
\end{array}\right)\left(\begin{array}{cc}
1 & -2 \\
-3 & 1
\end{array}\right)=\left(\begin{array}{cccc}
\begin{array}{ll}
1 & 2 \\
1 & 1
\end{array} & 2 & -2 \\
-3 & 3 & 1 \\
3 & 1 & 1 & 1 \\
1 & & & -2 \\
-3
\end{array}\right)=\left(\begin{array}{cc}
1-6 & -2+2 \\
3-3 & -6+1
\end{array}\right)=\left(\begin{array}{cc}
-5 & 0 \\
0 & -5
\end{array}\right) \\
& B A=\left(\begin{array}{cc}
1 & -2 \\
-3 & 1
\end{array}\right)\left(\begin{array}{ll}
1 & 2 \\
3 & 1
\end{array}\right)=\left(\begin{array}{cccc}
1 & -2 & 1 & -2 \\
3 & & 2 \\
3 & 1 & -3 & 1 \\
-3 & & 1 & 2 \\
3
\end{array}\right)=\left(\begin{array}{cc}
1-6 & 2-2 \\
-3+3 & -6+1
\end{array}\right)=\left(\begin{array}{cc}
-5 & 0 \\
0 & -5
\end{array}\right)
\end{aligned}
$$

Find the values of $x, y, z$ if $\quad\left(\begin{array}{cc}x-3 & 3 x-z \\ x+y+7 & x+y+z\end{array}\right)=\left(\begin{array}{ll}1 & 0 \\ 1 & 6\end{array}\right)$

Solution: | $\Rightarrow \mathrm{x}-3=1$ | $3 \mathrm{x}-\mathrm{z}=0$ |
| ---: | ---: | ---: |
| $\therefore \mathrm{x}=4$ | $12-\mathrm{z}=0$ |$\Rightarrow \mathrm{z}=12 \Rightarrow \begin{array}{r}x+y+7=1\end{array} \Rightarrow \quad \mathrm{x}+\mathrm{y}=-1$

$$
\therefore x=4 \mid 12-z=0 \Rightarrow z=12 \Rightarrow x+y=-6 \Rightarrow 4+y=-6 \Rightarrow y=-10
$$

If $A=\left(\begin{array}{lll}0 & 4 & 9 \\ 8 & 3 & 7\end{array}\right), B=\left(\begin{array}{lll}7 & 3 & 8 \\ 1 & 4 & 9\end{array}\right)$ find the value of $B-5 A$
Solution :

$$
\begin{aligned}
B-5 A=\left(\begin{array}{lll}
7 & 3 & 8 \\
1 & 4 & 9
\end{array}\right)-5\left(\begin{array}{lll}
7 & 3 & 8 \\
1 & 4 & 9
\end{array}\right)= & \left(\begin{array}{lll}
7 & 3 & 8 \\
1 & 4 & 9
\end{array}\right)-\left(\begin{array}{lll}
0 & 20 & 45 \\
40 & 15 & 35
\end{array}\right)=\left(\begin{array}{lll}
7 & 3 & 8 \\
1 & 4 & 9
\end{array}\right)+\binom{0-20-45}{-40-15-35} \\
& =\left(\begin{array}{lll}
7 & -17 & -37 \\
-39 & -11 & -26
\end{array}\right)
\end{aligned}
$$

If a matrix has 16 elements, what are the possible orders it can have?
Solution: The matrix has 16 elements. Hence possible orders are $1 \times 16,16 \times 1,4 \times 4,2 \times 8,8 \times 2$.
If $A=\left(\begin{array}{lll}1 & 2 & 0 \\ 3 & 1 & 5\end{array}\right), B=\left(\begin{array}{lll}8 & 3 & 1 \\ 2 & 4 & 1 \\ 5 & 3 & 1\end{array}\right)$ find $A B$
Solution :

$$
=\left(\begin{array}{ccc}
8+4+0 & 3+8+0 & 1+2+0 \\
24+2+25 & 9+4+15 & 3+1+5
\end{array}\right)=\left(\begin{array}{ccc}
12 & 11 & 3 \\
51 & 28 & 9
\end{array}\right)
$$

If $A=\left(\begin{array}{cc}2 & -2 \sqrt{2} \\ \sqrt{2} & 2\end{array}\right)$ and $B=\left(\begin{array}{cc}2 & 2 \sqrt{2} \\ -\sqrt{2} & 2\end{array}\right)$ Show that $A$ and $B$ satisfy commutative property
Solution

$$
\begin{aligned}
& A B=\left(\begin{array}{cc}
2 & -2 \sqrt{2} \\
\sqrt{2} & 2
\end{array}\right) \times\left(\begin{array}{cc}
2 & 2 \sqrt{2} \\
-\sqrt{2} & 2
\end{array}\right)=\left(\begin{array}{ll}
8 & 0 \\
0 & 8
\end{array}\right) \\
& B A=\left(\begin{array}{cc}
2 & 2 \sqrt{2} \\
-\sqrt{2} & 2
\end{array}\right) \times\left(\begin{array}{cc}
2 & -2 \sqrt{2} \\
\sqrt{2} & 2
\end{array}\right)=\left(\begin{array}{ll}
8 & 0 \\
0 & 8
\end{array}\right) \quad \text { A and B satisfy commutative property }
\end{aligned}
$$

Construct a $3 \times 3$ matrix whose elements are given by $a_{i j}=\frac{(i+j)^{3}}{3}$
Solution:

$$
\begin{array}{cc}
a_{11}=8 / 3, & a_{12}=27 / 3=9, \quad a_{13}=64 / 3 \quad a_{21}=27 / 3=9, a_{22}=64 / 3, \\
a_{23}=125 / 3 & a_{31}=64 / 3, \quad a_{32}=125 / 3, \quad a_{33}=216 / 3=72 \\
\therefore A & \\
\therefore\left(\begin{array}{ccc}
8 / 3 & 9 & 64 / 3 \\
9 & 64 / 3 & 125 / 3 \\
64 / 3 & 125 / 3 & 72
\end{array}\right)
\end{array}
$$

If $A=\left(\begin{array}{lll}1 & 8 & 3 \\ 3 & 5 & 0 \\ 8 & 7 & 6\end{array}\right), B=\left(\begin{array}{ccc}8 & -6 & -4 \\ 2 & 11 & -3 \\ 0 & 1 & 5\end{array}\right), C=\left(\begin{array}{ccc}5 & 3 & 0 \\ -1 & -7 & 2 \\ 1 & 4 & 3\end{array}\right)$ compute $3 A+2 B-C$
Solution :

$$
3 A+2 B-C=3\left(\begin{array}{lll}
1 & 8 & 3 \\
3 & 5 & 0 \\
8 & 7 & 6
\end{array}\right)+2\left(\begin{array}{ccc}
8 & -6 & -4 \\
2 & 11 & -3 \\
0 & 1 & 5
\end{array}\right)-\left(\begin{array}{ccc}
5 & 3 & 0 \\
-1 & -7 & 2 \\
1 & 4 & 3
\end{array}\right)
$$

$$
=\left(\begin{array}{ccc}
3 & 24 & 9 \\
9 & 15 & 0 \\
24 & 21 & 18
\end{array}\right)+\left(\begin{array}{ccc}
16 & -12 & -8 \\
4 & 22 & -6 \\
0 & 2 & 10
\end{array}\right)+\left(\begin{array}{ccc}
-5 & -3 & 0 \\
1 & 7 & -2 \\
-1 & -4 & -3
\end{array}\right)=\left(\begin{array}{ccc}
14 & 9 & 1 \\
14 & 44 & -8 \\
23 & 19 & 25
\end{array}\right)
$$

If $A=\left(\begin{array}{ccc}7 & 8 & 6 \\ 1 & 3 & 9 \\ -4 & 3 & -1\end{array}\right) \mathbf{B}=\left(\begin{array}{ccc}4 & 11 & -3 \\ -1 & 2 & 4 \\ 7 & 5 & 0\end{array}\right)$ then Find $2 A+B$
Solution: $2 A+B=2\left(\begin{array}{ccc}7 & 8 & 6 \\ 1 & 3 & 9 \\ -4 & 3 & -1\end{array}\right)+\left(\begin{array}{ccc}4 & 11 & -3 \\ -1 & 2 & 4 \\ 7 & 5 & 0\end{array}\right)=\left(\begin{array}{ccc}14 & 16 & 12 \\ 2 & 6 & 18 \\ -8 & 6 & -2\end{array}\right)+\left(\begin{array}{ccc}4 & 11 & -3 \\ -1 & 2 & 4 \\ 7 & 5 & 0\end{array}\right)=\left(\begin{array}{ccc}18 & 27 & 9 \\ 1 & 8 & 22 \\ -1 & 11 & -2\end{array}\right)$
Find the values of $x, y$ and $z$ from the following equations $\left(\begin{array}{cc}x+y & 2 \\ 5+z & x y\end{array}\right)=\left(\begin{array}{ll}6 & 2 \\ 5 & 8\end{array}\right)$
Solution:

$$
\left(\begin{array}{cc}
x+y & 2 \\
5+z & x y
\end{array}\right)=\left(\begin{array}{ll}
6 & 2 \\
5 & 8
\end{array}\right) \underset{ }{\Rightarrow x+y=6,} \begin{array}{cl}
x y=8 \\
x=2(0 r) 4 & y=4(0)
\end{array}
$$

$$
x=2 \text { (or) } 4, \quad y=4 \text { (or) } 2 \quad 5+z=5 \Rightarrow z=0
$$

Find the values of $x$, $y$ and $z$ from the following equations $\left(\begin{array}{ll}12 & 3 \\ x & \frac{3}{2}\end{array}\right)=\left(\begin{array}{ll}y & z \\ 3 & 5\end{array}\right)$
Solution: $\quad\left(\begin{array}{ll}12 & 3 \\ & 3\end{array}\right)=\left(\begin{array}{ll}y & z\end{array}\right) \Rightarrow x=3, y=12$,

$$
\left(\begin{array}{ll}
12 & 3 \\
x & \frac{3}{2}
\end{array}\right)=\left(\begin{array}{ll}
y & z \\
3 & 5
\end{array}\right) \Rightarrow x=3, y=12, z=3
$$

## 4.GEOMETRY

Write the Ceva's Theorem
Let $A B C$ be a triangle and let $D, E, F$ be points on lines $B C, C A, A B$ respec tively. Then the cevians $A D, B E$, CF are concurrent if and only if $\frac{B D}{D C} \times \frac{C E}{E A} \times \frac{A F}{F B}=1$ where the lengths are directed

## PQ is a tangent drawn from a point $P$ to a circle with centre $O$ and $Q O R$ is a diameter of the circle such

 that $\angle \mathbf{P O R}=120^{\circ}$. Find $\angle \mathrm{OPQ}$.Solution: Given $\angle \mathrm{POR}=120^{\circ} \Rightarrow \angle \mathrm{POQ}=60^{\circ}$ (linear pair)

$$
\begin{aligned}
& \angle \mathrm{OQP}=90^{\circ} \text { (Radius } \perp \text { tangent) } \\
& \therefore \angle \mathrm{OPQ}=90^{\circ}-60^{\circ}=30^{\circ}
\end{aligned}
$$



If $\triangle A B C$ is similar to $\triangle D E F$ such that $B C=3 \mathrm{~cm}, E F=4 \mathrm{~cm}$ and area of $\triangle A B C=54 \mathrm{~cm}^{2}$. Find the area of $\triangle \mathrm{DEF}$
Solution : $\frac{\text { Area }(\triangle A B C)}{\text { Area }(\triangle D E F)}=\frac{B C^{2}}{E F^{2}} \Rightarrow \frac{54}{\text { Area }(\triangle D E F)}=\frac{3^{2}}{4^{2}} \Rightarrow \frac{54}{\text { Area }(\triangle D E F)}=\frac{9}{16} \Rightarrow$ Area $(\triangle D E F)=\frac{16 \times 54}{9}=96 \mathrm{~cm}^{2}$
In Fig. QA and $P B$ are perpendiculars to $A B$. If $A O=10 \mathrm{~cm}, B O=6 \mathrm{~cm}$ and $P B=9 \mathrm{~cm}$. Find $A Q$.
Solution :

$$
A Q=\frac{10 \times 9}{6}=15 \mathrm{~cm}
$$



## Write the Menelaus Theorem

A necessary and sufficient condition for points $P, Q, R$ on the respective sides $B C, C A, A B$ of a triangle $A B C$ to be collinear is that $\frac{B P}{P C} \times \frac{C Q}{Q A} \times \frac{A R}{R B}=1$ where all segments in the formula are directed segments.

## Write the Alternate Segment theorem

The angles between the tangent and the chord are equal to the angles in the corresponding alternate segments.

## If $\triangle \mathrm{ABC} \sim \triangle \mathrm{DEF}$ such that area of $\triangle \mathrm{ABC}$ is $9 \mathrm{~cm}^{2}$ and the area of $\triangle \mathrm{DEF}$ is $16 \mathrm{~cm}^{2}$ and $\mathrm{BC}=\mathbf{2 . 1} \mathrm{cm}$

## Find the length of EF.

Solution : $\therefore \frac{\text { Area of } \triangle A B C}{\text { Area of } \triangle D E F}=\frac{B C^{2}}{E F^{2}}$
$\Rightarrow \frac{9}{16}=\frac{(2.1)^{2}}{E F^{2}}$
$\therefore \quad E F=\frac{4 \times 2.1}{3}=2.8 \mathrm{~cm}$
Check whether $A D$ is bisector of $\angle A$ of $\triangle A B C, A B=4 \mathrm{~cm}, A C=6 \mathrm{~cm} . B D=1.6 . \mathrm{cm}$ and CD $=2.4 \mathrm{~cm}$.
Solution:

$$
\frac{A B}{A C}=\frac{4}{6}=\frac{2}{3}, \frac{B D}{D C}=\frac{1.6}{2.4}=\frac{2}{3}
$$

$$
\therefore \text { By Converse of ABT, } \therefore \frac{A B}{A C}=\frac{B D}{D C}
$$

AD is the bisector of $\angle \mathrm{A}$.

## The length of the tangent to a circle from a point $P$, which is $\mathbf{2 5} \mathbf{~ c m}$ awny from the centre is $\mathbf{2 4} \mathbf{~ c m}$.

 What is the radius of the circle?Solution: $\therefore O T=\sqrt{25^{2}-24^{2}}=\sqrt{625-576}=\sqrt{49}=7 \mathrm{~cm}$

$$
\therefore \text { Radius }=7 \mathrm{~cm}
$$



In Figure $O$ is the centre of a circle. $P Q$ is a chord and the tangent $P R$ at $P$ makes an angle of $50^{\circ}$ with PQ. Find $\angle P O Q$
Solution : $\angle O P Q=90^{\circ}-50^{\circ}=40^{\circ} \quad O P=O Q$ (Radii of a circle are equal)
$\angle \mathrm{OPQ}=\angle \mathrm{OQP}=40^{\circ}(\triangle \mathrm{OPQ}$ is isosceles $)$
$\angle \mathrm{POQ}=180^{\circ}-\angle \mathrm{OPQ}-\angle \mathrm{OQP}$
$\angle \mathrm{POQ}=180^{\circ}-40^{\circ}-40^{\circ}=100^{\circ}$
A tangent ST to a circle touches it at B . AB is a chord such that $\angle \mathrm{ABT}=65^{\circ}$. Find $\angle \mathrm{AOB}$, where " $O$ " is the centre of the circle.
Solution: $\quad \angle \mathrm{TBA}=65^{\circ} \Rightarrow \angle \mathrm{APB}=65^{\circ}$ (angles in altemate segment).
$\therefore \angle \mathrm{AOB}=2 \angle \mathrm{APB}=2\left(65^{\circ}\right)=130^{\circ}$


Find the volume of a cylinder whose height is 2 m and whose base area is $250 \mathrm{~m}^{2}$.
Solution : Let r and h be the radius and height of the cylinder respectively.

$$
\text { height } \mathrm{h}=2 \mathrm{~m}, \quad \text { base area }=250 \mathrm{~m}^{2}
$$

volume of a cylinder $=\pi r^{2} h \mathrm{cu}$. units

$$
\begin{aligned}
& =\text { base area } \times \mathrm{h} \\
& =250 \times 2=500 \mathrm{~m}^{3}
\end{aligned}
$$

## 5.COORDINATE GEONETRY

Find the intercepts made by the line $4 x-9 y+36=0$ on the coordinate axes.
Solution : put $x=0 \Rightarrow 4 x=-36 \quad x$ intercept $a=-9$
put $\quad y=0 \Rightarrow-9 y+36=0 .-9 y=-36 \Rightarrow y$ intercept $b=4$
Show that the straight lines $2 x+3 y-8=0$ and $4 x+6 y+18=0$ are parallel.
Solution:
Slope of the straight line $2 x+3 y-8=0$ is $\quad m_{1}=\frac{\text {-coefficient of } x}{\text { coefficient of } y}=\frac{-2}{3}$
Slope of the straight line $4 x+6 y+18=0$ is $\quad m_{2}=\frac{-4}{6}=\frac{-2}{3} \quad$ Here, $m_{1}=m_{2}$
That is, slopes are equal. Hence, the two straight lines are parallel.
Find the equation of a straight line which is parallel to the line $3 x-7 y=12$ and passing through the point $(6,4)$.
Solution: Equation of the straight line, parallel to $3 x-7 y-12=0$ is $3 x-7 y+k=0$

$$
3(6)-7(4)+k=0 \Rightarrow k=28-18=10
$$

The required straight line is $3 x-7 y+10=0$
Find the equation of a straight line perpendicular to the line $y=\frac{4}{3} x-7$ and passing through the point (7, - 1).
Solution:
The equation $y=\frac{4}{3} x-7 \Rightarrow 4 x-3 y-21=0$.
Equation of a straight line perpendicular to $4 x-3 y-21=0$ is $3 x+4 y+k=0$
it is passes through the point $(7,-1), \quad 21-4+k=0 \Rightarrow k=-17$
The required straight line is $3 x+4 y-17=0$.
Find the slope and $y$ intercept of $\sqrt{3} x+(1-\sqrt{3}) y=3$.
Sohution : $a=\sqrt{3} \quad b=(1-\sqrt{3}) \quad c=-3$
Slope of the line $=\frac{-a}{b}=\frac{-\sqrt{3}}{(1-\sqrt{3})}=\frac{3+\sqrt{3}}{2}$
Interecept on $y$-axis $=\frac{-c}{b}=\frac{-(-3)}{1-\sqrt{3}}=\frac{3+3 \sqrt{3}}{-2}$
Find the equation of a line whose inclination is $30^{\circ}$ and making an intercept -3 on the $Y$ axis.
Solution : Given $\theta=30^{\circ} \Rightarrow m=\tan 30^{\circ}=\frac{1}{\sqrt{3}}$ and $y$-intercept $=-3$
The required equation of the line is $\quad y=m x+c \Rightarrow y=\frac{1}{\sqrt{3}} x-3 \Rightarrow \sqrt{3} y=x-3 \sqrt{3}$
Find the equation of a Hine through the given pair of points $\left(2, \frac{2}{3}\right)$ and $\left(\frac{-1}{2},-2\right)$
Solution : Given points are $\left(2, \frac{2}{3}\right) \cdot\left(\frac{-1}{2},-2\right)$ two-point form $\frac{y-y_{1}}{y_{2}-y_{1}}=\frac{x-x_{1}}{x_{2}-x_{1}}$

$$
\frac{y-\frac{2}{3}}{-2-\frac{2}{3}}=\frac{x-2}{\frac{-1}{2}-2} \Rightarrow \frac{3 y-2}{-8}=\frac{x-2}{\frac{-5}{2}} \Rightarrow \frac{3 y-2}{-8}=\frac{2 x-4}{-5} \Rightarrow
$$

Find the equation of a straight line whose Slope is 5 and $x$ intercept is -9
Solution: Given, Slope $=5, x$ intercept, $d=-9$
The equation of a straight line is $y=m(x-d) \quad y=5(x+9) \quad y=5 x+45$
Find the equation of a line passing through the point $(3,-4)$ and having slope $\frac{-5}{7}$
Solution : Given slope of the line is $-\frac{5}{7}$ and $(3,-4)$ is a point on the line.

$$
y-y_{1}=m\left(x-x_{1}\right) \Rightarrow y+4=\frac{-5}{7}(x-3) \Rightarrow 5 x+7 y+13=0 .
$$

Find the equation of a straight line which has slope $\frac{-5}{4}$ and passing through the point $(-1,2)$.
Solution : slope of the line is $\frac{-5}{4}$ and $(-1,2)$ is a point on the line.

$$
y-y_{1}=m\left(x-x_{1}\right) \Rightarrow y-2=\frac{-5}{4}(x+1) \Rightarrow 4 y-8=-5 x-5 \Rightarrow 5 x+4 y-3=0
$$

Find the equation of a stralght line passing through the mid-point of a line segment joining the points $(1,-5),(4,2)$ and parallel to (i) $X$ axis (ii) $Y$ axis
Solution : Mid point of the line joining the points $(1,-5),(4,2)$ is

$$
=\left[\frac{x_{1}+x_{2}}{2}, \frac{y_{1}+y_{2}}{2}\right]=\left(\frac{1+4}{2}, \frac{-5+2}{2}\right)=\left(\frac{5}{2}, \frac{-3}{2}\right)
$$

$\begin{array}{ll}\text { (i) Parallel to } x \text {-axis is } y=-3 / 2 & \text { (ii) Parallel to } y \text {-axis is } x=5 / 2\end{array}$
Find the slope of a line joining the given points $(14,10)$ and $(14,-6)$
Solution: The slope $=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{(-6)-(10)}{(14)-(14)}=\frac{-6-10}{14-14}=\frac{-16}{0}$. The slope is undefined.

## 7NIENEURATION

If the base area of a hemispherical solid is 1386 sq. metres, then find its total surface area?
Solution : Let r be the radius of the hemisphere. $\pi \mathrm{r}^{2}=1386 \mathrm{sq} . \mathrm{m}$

$$
\text { T.S.A. }=3 \pi \mathrm{r}^{2} \mathrm{sq} . \mathrm{m}=3 \times 1386=4158 \mathrm{~m}^{2} .
$$

Find the diameter of a sphere whose surface area is $154 \mathrm{~m}^{2}$.
Solution : Let r be the radius of the sphere
Given that, $4 \pi r^{2}=154 \Rightarrow 4 \times \frac{22}{7} \times r^{2}=154 \Rightarrow r=\frac{7}{2} \Rightarrow$ Diameter $=7 \mathrm{~m}$

The curved surface area of a right circular cylinder of height 14 cm is $88 \mathrm{~cm}^{2}$. Find the diameter of the cylinder
Solution : C.S.A. of the cylinder $=88 \mathrm{sq} . \mathrm{cm} \Rightarrow 2 \pi \mathrm{rh}=88 \mathrm{~cm}^{2}$.

$$
\begin{aligned}
2 \times \frac{22}{7} \times r \times 14 & =88(\text { given } h=14 \mathrm{~cm}) \\
2 r & =\frac{88 \times 7}{22 \times 14}=2 \Rightarrow \text { Diameter }=2 \mathrm{~cm}
\end{aligned}
$$

If the total surface area of a cone of radius 7 cm is $704 \mathrm{~cm}^{2}$, then find its slant height.
Solution : Given that, radius $\mathrm{r}=7 \mathrm{~cm}$
T.S.A. $=\pi r(l+\mathrm{r}) \mathrm{sq}$. units $\Rightarrow 704=\frac{22}{7} \times 7(l+7) \Rightarrow 32=l+7 \Rightarrow l=25 \mathrm{~cm}$

The slant height of the cone is 25 cm .

An aluminium sphere of radius $\mathbf{1 2} \mathbf{c m}$ is melted to make a cylinder of radius $\mathbf{8 ~ c m}$. Find the height of the cyifinder.
Solution: Given radius of sphere $=12 \mathrm{~cm}=\mathrm{R}$ \& radius of cylinder $=8 \mathrm{~cm}=\mathrm{r}$ Volume of sphere $=$ Volume of Cylinder

$$
\begin{gathered}
\frac{4}{3} \pi R^{3}=\pi r^{2} h \\
\frac{4}{3} \times 12 \times 12 \times 12=8 \times 8 \times h \Rightarrow h=36 \mathrm{~cm}
\end{gathered}
$$

## - EMAMEMCS AND PROBABILEI

Find the range and coefficient of range of the fol lowing data: $25,67,48,53,18,39,44$.
Solution : $\mathrm{L}=67 ; \mathrm{S}=18$

$$
\mathrm{R}=\mathrm{L}-\mathrm{S}=67-18=49 \text { and Coefficient of range }=\frac{L-S}{L+S}=\frac{67-18}{67+18}=\frac{49}{85} \text { (or) } 0.576
$$

The range of a set of data is 13.67 and the largest value is 70.08 . Find the smallest value.

## Solution : $\quad \quad \mathrm{R}=13.67 ; \mathrm{L}=70.08$

$R=L-S \Rightarrow 13.67=70.08-S \Rightarrow S=70.08-13.67=56.41 \Rightarrow$ The smallest value is 56.41 . Find the range and coefificient of range of $\mathbf{6 3}, \mathbf{8 9}, \mathbf{9 8}, \mathbf{1 2 5}, 79,108,117,68$

## Solution:

Range $=L-S=125-63=62$ and Coefficient of range $=\frac{L-S}{L+S}=\frac{125-63}{125+63}=\frac{62}{185}$ (or) 0.33

## Find the range and coefficient of range of $43.5,13.6,18.9,38.4,61.4,29.8$

Sohution:
Solution:
Range $=L-S=61.4-13.6=47.8 \quad$ Coefficient of range $=\frac{L-S}{L+S}=\frac{61.4-13.6}{61.4+13.6}=\frac{47.8}{75}$ (or)0.64
If the range and the smallest value of a set of data are 36.8 and 13.4 respectively, then find the largest value.
Solution: $\mathbf{R}=36.8 ; \mathbf{S}=13.4 \quad \therefore \mathrm{R}=\mathrm{L}-\mathrm{S} \Rightarrow 36.8=\mathrm{L}-13.4 \quad \therefore \mathrm{~L}=36.8+13.4=50.2$

Solution : $\mathrm{L}=650$; $\mathrm{S}=450$
. Range $=\mathrm{L}-\mathrm{S}=650-400=250$
A wall clock strikes the bell once at $10^{\prime}$ clock, 2 times at $20^{\prime}$ clock, 3 times at $30^{\prime}$ clock and so on.
How many times will it strike in a particular day. Find the standard deviation of the number of strikes the bell make a day.
Solution : $\therefore$ Number of times it strikes in a particular day $=2(1+2+3+\ldots \ldots . . .12)=2\left(\frac{12 \times 13}{2}\right)=156$ times
S.D of $2(1,2,3, \ldots \ldots .12)=2\left[\sqrt{\frac{n^{2}-1}{12}}\right]=2\left[\sqrt{\frac{144-1}{12}}\right]=2 \sqrt{\frac{143}{12}}=6.9$

Find the standard deviation of first 21 natural numbers.
Solution:
SD of first 21 natural numbers $=\sqrt{\frac{n^{2}-1}{12}}=\sqrt{\frac{441-1}{12}}=\sqrt{\frac{440}{12}}=6.05$
Find the standard deviation of irst 13 natural numbers.
Solution:
SD of first 21 natural numbers $=\sqrt{\frac{n^{2}-1}{12}}=\sqrt{\frac{169-1}{12}}=\sqrt{\frac{168}{12}}=3.74$

If $n=5, \bar{x}=6, \Sigma x^{2}=765$, then calculate the coefficient of variation.
Solution : Given $n=5, \bar{x}=6, \Sigma x^{2}=765, C V=$ ?

$$
\begin{aligned}
& \sigma=\sqrt{\frac{\sum x^{2}}{n}-\left(\frac{\sum x}{n}\right)^{2}}=\sqrt{\frac{765}{5}-(6)^{2}}=10.82 \\
& \therefore C . V=\frac{\sigma}{x} \times 100=\frac{10.82}{6} \times 100=180.33 \%
\end{aligned}
$$

If the range and coefinient of range of the data are 20 and 0.2 respectively, then find the largest and smallest values of the data.

$$
\text { Solution: } L-S=20 \quad \ldots(1) \quad L+S=100 \quad \ldots(2
$$

$$
\text { Solviong (1) and (2) } L=60, \quad S=40
$$

What is the probability that a leap year selected at random will contain 53 saturdays. (Hint: $366=52 \times 7+2$ ) Solution : $S=\{($ Sun-Mon, Mon-Tue, Tue-Wed, Wed-Thu, Thu-Fri, Fri-Sat, Sat-Sun) $\Rightarrow \mathrm{n}(\mathrm{S})=7$

$$
\text { Let } A \text { be the event of getting } 53^{\text {rd }} \text { Saturday. }
$$

$$
\mathrm{A}=\{\text { Fri-Sat, Sat-Sum }\} ; \mathrm{n}(\mathrm{~A})=2 \Rightarrow P(A)=\frac{2}{7}
$$

A die is rolled and a coin is tossed simultaneously. Find the probability that the die shows an odd number and the coin shows a head.
Solution : $S=\{1 \mathrm{H}, 1 \mathrm{~T}, 2 \mathrm{H}, 2 \mathrm{~T}, 3 \mathrm{H}, 3 \mathrm{~T}, 4 \mathrm{H}, 4 \mathrm{~T}, 5 \mathrm{H}, 5 \mathrm{~T}, 6 \mathrm{H}, 6 \mathrm{~T}\} ; \mathrm{n}(\mathrm{S})=12$
Let $A$ be the event of getting an odd number and a head
$\mathrm{A}=\{1 \mathrm{H}, 3 \mathrm{H}, 5 \mathrm{H}\} ; \mathrm{n}(\mathrm{A})=3 \Rightarrow P(A)=\frac{3}{12}=\frac{1}{4}$
A bag contains 6 green balls, some black and red balls. Number of black balls is as twice as the number of red balls. Probability of getting a green ball is thrice the probability of getting a red ball. Find (i) number of black balls (ii) total number of balls.
Solution : It is given that, $\mathrm{P}(\mathrm{G})=3 \times \mathrm{P}(\mathrm{R}) \Rightarrow \frac{6}{6+3 x}=3 \times \frac{x}{6+3 x}$

$$
3 x=6 \Rightarrow x=2
$$

(i) Number of black balls $=2 \times 2=4$
(ii) Total number of balls $=6+(3 \times 2)=12$

Two coins are tossed together. What is the prob ability of getting different faces on the coins? Solution : $\mathrm{S}=\{\mathrm{HH}, \mathrm{HT}, \mathrm{TH}, \mathrm{TT}\} ; \mathrm{n}(\mathrm{S})=4$
Let $A$ be the event of getting different faces on the coins.

$$
\mathrm{A}=\{\mathrm{HT}, \mathrm{TH}\} ; \mathrm{n}(\mathrm{~A})=2 \Rightarrow P(A)=\frac{2}{4}=\frac{1}{2}
$$

A bag contains 5 blue balls and 4 green balls. $A$ ball is drawn at random from the bag. Find the probability that the ball drawn is (i) blue (ii) not blue.
Solution : Total number of possible outcomes
$n(S)=5+4=9$
$n(S)=5+4=9$
(i) Let $A$ be the event of getting a blue ball. $\quad P(A)=\frac{5}{9}, ~$
(ii) $\bar{A}$ will be the event of not getting a blue ball. $P(\bar{A})=\frac{4}{9}$

A bag contains 5 white and some black balls. If the probablity of drawing a black ball from the bag is twice the probability of drawing a white ball then find the number of black balls.
Solution : Given $\mathrm{n}(\mathrm{S})=5+x, \quad 5$ white balls and $x$ black balls
By daa given, $P(B)=2 . P(W) \Rightarrow \frac{x}{5+x}=2 \cdot\left(\frac{5}{5+x}\right) \Rightarrow x=10 \quad \therefore$ No. of black balls $=10$
A coin is tossed thrice. What is the probability of getting two consecutive tails?
Solution : $\quad \mathrm{S}=\{(\mathrm{HHH})$, (HHT), (HTH), (HTT), (THH), (THT). (TTH), (TTT) $\} \Rightarrow n(S)=8$
Let A bet the event of getting 2 tails $A=\{(\mathrm{HTT})$. (TTH), (TTT) $\} \Rightarrow \mathrm{n}(\mathrm{A})=3 \Rightarrow P(A)=\frac{3}{8}$
Write the sample space for tossing three coins using tree diagram. Solution :
$\mathrm{S}=\{(\mathrm{HHH}),(\mathrm{HHT}),(\mathrm{HTH}),(\mathrm{HTT}),(\mathrm{THH}),(\mathrm{THT}),(\mathrm{TTH}),(\mathrm{TTT})\}$
Write the sample space for selecting two bails from a bag containing 6 balls num

| $\begin{array}{l}\text { bered } 1 \text { to } 6 \text { (using tree diagram). } \\ \text { Solution : } \\ \text { (same answer also) }\end{array}$ |
| :--- | :--- |
| $\mathbf{S}=\{(1,1),(1,2),(1,3),(1,4),(1,5),(1,6),(2,1),(2,2),(2,3),(2,4),(2,5),(2,6)$ |
| $(3,1),(3,2),(3,3),(3,4),(3,5),(3,6),(4,1),(4,2),(4,3),(4,4),(4,5),(4,6)$ |

$(3,1),(3,2),(3,3),(3,4),(3,5),(3,6),(4,1),(4,2),(4,3),(4,4),(4,5),(4,6)$
$(5,1),(5,2),(5,3),(5,4),(5,5),(5,6),(6,1),(6,2),(6,3),(6,4),(6,5),(6,6)\}$
If the standard deviation of a data is $\mathbf{4 . 5}$ and if each value of the data is decreased by $\mathbf{5}$, then find the new standard devia tion.
Solution : $S . D$ of a data $=4.5 \Rightarrow$ new S.D of a data $=4.5$
( $\because$ SD will not be changed when we add (or) subtract fixed constant to all the values of the data) If the standard deviation of a data is 3.6 and each value of the data is divided by 3 , then find the new variance and new standard deviation.
Solution : S.D of a data $=3.6 \Rightarrow$ new S.D $=\frac{3.6}{3}=1.2$

$$
\text { New Variance }=(1.2)^{2}=1.44
$$

The mean of a data is 25.6 and its coefficient of variation is 18.75 . Find the standard deviation
Solution : Mean $\bar{x}=25.6$, Coefficient of variation, C.V. $=18.75$

$$
\text { Coefficient of variation, C.V. }=\frac{\sigma}{x} \times 100 \% \Rightarrow 18.75=\frac{\sigma}{25.6} \times 100 \Rightarrow \sigma=4.8
$$

The standard deviation and mean of a data are 6.5 and 12.5 respectively. Find the coefficient
of variation.
Solution : $\sigma=6.5, \bar{x}=12.5 \quad \therefore C . V=\frac{\sigma}{\bar{x}} \times 100=\frac{6.5}{12.5} \times 100=52 \%$
The standard deviation and coefificient of variation of a data are 1.2 and 25.6 respectively. Find the value of mean.
Solution : Given $\sigma=1.2, C . V=25.6 \quad \therefore C . V=\frac{\sigma}{\bar{x}} \times 100 \Rightarrow 25.6=\frac{1.2}{\bar{x}} \times 100 \Rightarrow \bar{x}=\frac{120}{25.6}=4.69$
If the mean and coefficient of variation of a data are 15 and 48 respectively, then find the value of standard deviation.
Solution : Given $\bar{x}=15, C V=48, \sigma=? \quad \therefore C . V=\frac{\sigma}{x} \times 100 \Rightarrow 48=\frac{\sigma}{15} \times 100 \Rightarrow \sigma=\frac{15 \times 48}{100}=7.2$
In a two children family, find the probability that there is at least one girl in a family. Solution : $S=\{(B B),(B G),(G B),(G G)\} \Rightarrow n(S)=4$
Let $A$ be the event of getting atleast one girl. $A=\{(B G),(G B),(G G)\} \Rightarrow \therefore n(A)=3$

$$
\begin{aligned}
& \Rightarrow \quad \therefore(A)=3 \\
& \Rightarrow P(A)=\frac{3}{4}
\end{aligned}
$$

